0. Introduction

In the past four decades, the field of sentence processing research has generated a number of models of the incremental operation of the human sentence processor. One assumption common to most of these theories is that the difficulty of a word is determined by the possible syntactic structures of the preceding words, and thus, the difficulty of a word should be unaffected by ungrammatical analyses of the preceding words. Put formally, the difficulty of word $w_n$ of a sentence is determined only by the grammatical syntactic structures covering the preceding words $w_1 \cdots w_{n-1} (\equiv w_1^{n-1})$. Recent results by Tabor, Galantucci, and Richardson (2004), however, appear to show evidence of a case where a syntactic structure which is not possible given $w_1^{n-1}$ nevertheless influences the difficulty of $w_n$. They attribute such effects to ‘merely locally coherent’ syntactic structures and term such impossible structures local coherences. Follow-up studies by Konieczny (2005) and Konieczny and Müller (2006, 2007) provide further evidence that these impossible structures are being constructed and even semantically evaluated. These results have been taken to support a small class of dynamical systems models of sentence processing (e.g., Tabor and Hutchins 2004), in which, crucially, structures which are not possible given the current input are nevertheless constructed and compete with other, tenable structures. Unfortunately, the existing theories in this class have a large number of interacting free parameters, making interpretation somewhat difficult and leaving unspecified how to scale up such a system to make broad-coverage reading time predictions. This paper fills two gaps in the literature on local coherences. First, it demonstrates from two experiments with an eye-tracking corpus that effects of local coherences are evident in the reading of naturalistic text. Second, it describes a new computational model of local coherences that is motivated by a view of sentence processing as updating prior beliefs over syntactic structures.

0.1. Local Coherences: The Initial Result

The first study to report effects of local coherences is described in Tabor, Galantucci, and Richardson (2004). In Experiment 1, they use a self-paced reading task and materials containing relative clauses (RCs) attached to nouns in non-subject
Their experimental design crossed RC reduction with verb ambiguity. RCs are either reduced (1a,c) or unreduced (1b,d), and the RC verb is either lexically ambiguous between a past tense active and a past participle (1a–b), or is unambiguously a past participle (1c–d).

Tabor, Galantucci, and Richardson point out that in one of these four conditions (1a) there is a locally coherent string *the player tossed a frisbee*. Out of context (e.g., if it were starting a sentence) this string would have a likely parse in which *the player* is the agent of *tossed* and *a frisbee* is the theme. Given the preceding context, however, *the player* is in non-subject position and thus this parse is impossible. That is, given the preceding context, *the player tossed the frisbee* must begin a reduced RC, and there is no local ambiguity. Thus, so long as ungrammatical analyses are not considered, (1a) should be no more difficult than the other examples, except insofar as ambiguous verbs are harder than unambiguous verbs, and reduced RCs are harder than unreduced RCs. That is, the prediction for reading times in the *tossed a frisbee by* region from most theories of sentence processing would be to get the two main effects of RC reduction and verb ambiguity.

Tabor, Galantucci, and Richardson, however, predict an interaction such that (1a) will have added difficulty above and beyond these two effects, because of the interference from the locally coherent parse of *the player tossed a frisbee*. Concordant with their predictions, they find an interaction in the *tossed a frisbee by* region, such that reading times for (1a) are super-additively high, suggesting that ungrammatical analyses are considered by the human sentence processor.

### 0.2. Local Coherences: Theories

With the results showing effects of local coherences in mind, we can ask the question of what sorts of theories predict these effects. This section briefly describes two recent examples of such theories. The first involves dynamical systems models to explain the effects, while the second uses a mathematical model of the combination of bottom-up and top-down probabilistic information.

Tabor and Hutchins (2004) describes the SOPARSE (self-organized parse) model, in which reading a word activates a set of lexically anchored tree fragments. These tree fragments then compete, spreading activation to compatible fragments and inhibiting incompatible fragments, such that the system eventually stabilizes to the correct parse. Reading times for each word can then be modeled as the time the system takes to stabilize after reading a word. Stabilization takes longer for locally coherent regions because the locally coherent parse is created and competes with the globally grammatical parses, thus nicely explaining the results on local coherences.
Correcting the Incorrect

There are, however, unsolved issues with this model. The model has a number of free parameters, relating to the equations used for the competition, the method by which links between fragments are formed, as well as the question of precisely what tree fragments a given word will activate. While Tabor and Hutchins (2004) works out these questions in detail for the types of sentences they model, it is unclear how to scale the model up to make predictions for arbitrary types of sentences. That is, there is no principled system for setting the three types of parameters mentioned, and no clear interpretation of their values. The model put forward in this paper is an attempt to remedy this situation.

A recent proposal by Gibson (2006) can also explain some of the local coherence results. Gibson’s proposal is that part-of-speech ambiguities have a special status in parsing; in effect, lexical part-of-speech ambiguities can be thought of as one-word local coherences. In this model, a lexical bias ($LB$) is created for each part-of-speech tag $t_i$ of word $w$ by multiplying together the context-independent probability of $t_i$ given the word $w$ (the bottom-up component) by a smoothed probability of the tag given the context (the top-down component):

\begin{equation}
LB(t_i) = P(t_i|w)Ps(t_i|\text{context})
\end{equation}

$Ps$ is smoothed by adding .01 to the probability of every tag $t \in T$, such that it no longer sums to one, and is thus not a true probability function. Then, a true probability is calculated for each tag $t_i$ by normalizing the $LB$ terms:

\begin{equation}
P(t_i) = \frac{LB(t_i)}{\sum_{i \in T} LB(t)}
\end{equation}

Gibson describes two ways in which the resultant probabilities can be used to predict difficulty, one for serial and one for parallel models. For serial models, the parser stochastically selects a part-of-speech for the current word from the $P(t)$ distribution. When the part-of-speech it selects cannot be integrated into the current syntactic representation, difficulty occurs from reanalysis. In a parallel model, the parser maintains all possibilities for the part-of-speech of the word, weighted by $P(t)$. In cases where multiple parts of speech have positive probabilities, competition ensues.

Because the top-down probabilities are smoothed to allow for all possible parts-of-speech, any word which is lexically ambiguous will be more difficult to process, regardless of whether it is ambiguous or not in its context. This can thus explain some of the difference between the ambiguous and unambiguous verbs in Tabor, Galantucci, and Richardson (2004). It is not clear, however, under such a model why the super-additive interaction would obtain. Furthermore, such a theory cannot at all explain the semantic effects of local coherences, such as those described in Tabor, Galantucci, and Richardson’s (2004) Experiment 2, or the visual world results of Konieczny and Müller (2006, 2007). In addition, Gibson’s model is a bit underspecified: he does not discuss how the top-down probabilities are calculated, nor
Klinton Bicknell, Roger Levy, and Vera Demberg

what the precise linking hypothesis is between the final $P(t)$ and reading times. Finally, it is not at all clear why the top-down expectations should be smoothed, since the smoothing actually has negative consequences on the processor’s performance.

0.3. Goals
The goals of this paper are twofold. The first goal concerns the empirical status of effects of local coherences. All of the extant results on the phenomenon involve controlled experiments, most of which crucially involve very rare types of constructions. For example, the result of Tabor, Galantucci, and Richardson (2004) relies on reduced relative clauses formed from a passivization on the recipient of a ditransitive construction. Such a type of sentence is quite rare in English, and thus might not give useful insight into the normal operation of the sentence processor. This paper presents the results of two experiments with a corpus of eye-tracking data from the reading of newspaper articles demonstrating effects of local coherences in the reading of naturalistic sentences. This establishes the ecological validity of the study of local coherences, and underscores the need for a theory of local coherences which makes broad-coverage predictions. The second goal of this paper is to present a model of the effects of local coherences that combines the strengths of Gibson’s (2006) and Tabor and Hutchins’s (2004) models. This model accounts for phrasal-level effects of local coherences (as Tabor and Hutchins), but does so using general quantities that can be calculated for any sentence type (as Gibson) by using a general probabilistic parser that can operate on any SCFG. The remainder of this paper is divided into four sections. The next two sections present the two corpus experiments. Following that, we present our model and conclude.

1. Experiment 1
The basic strategy of the two corpus experiments is to build a regression model of the reading times on each word in an eye-tracking corpus. Included in the regression model for each experiment is a factor quantifying the occurrence of local coherences. Establishing that local coherences have an effect on reading times is then merely a matter of assessing the significance of the local coherences factor in the model, and assessing the size of that effect is merely a matter of inspecting the coefficient estimate.

The local coherences factor in Experiment 1 is meant to start simple by measuring the effect of one-word local coherences. Although *prima facie*, one-word local coherences do not seem to look much like the materials in Tabor, Galantucci, and Richardson (2004), the reasoning for calling them local coherences is as follows: we take the definition of a local coherence to be a string of words $w$ that out of context would suggest one very likely parse, and that parse is impossible (or at least highly unlikely) in context. We can scale this down to the case where $w$ is a string of size 1; that is, out of context, a word $w$ suggests a very likely parse (e.g., a part-of-speech tag) that is very unlikely or impossible in context. Because a word only has one part-of-speech in a given sentence, this means we can invert this statement to say that a one-word local coherence occurs when the only possible part-of-speech tag
Correcting the Incorrect

for the word in context is highly unlikely out of context. By making the assumption that the only possible part-of-speech tag for a word in context can be approximated by the actual part-of-speech tag the word has in the sentence, we can calculate our one-word local coherence factor to be an estimate of the context-independent probability of the actual part-of-speech tag $t_i$ for a word $w_i$ given just the word $P(t_i|w_i)$. This factor will thus be low when there is a strong one-word local coherence.

This particular type of one-word local coherence is predicted to have an effect by both Gibson’s (2006) and Tabor and Hutchins’s (2004) models. This probability is actually one of the components in the Gibson theory, which would predict that – all else being equal – a word $w_i$ would be read more slowly as $P(t_i|w_i)$ decreases. Just as Gibson’s theory would predict, this factor would assign lower probability to tossed tagged as a past participle than it would thrown tagged as a past participle. A dynamical systems model such as Tabor and Hutchins’s makes the same prediction if we assume that the strength of the lexically-anchored tree fragments corresponding to each part-of-speech vary in strength in proportion to $P(t_i|w_i)$, which seems to be a reasonable interpretation of what their model would involve. Of course, this factor doesn’t capture local coherences at a phrasal level, as Tabor and Hutchins would predict. The next experiment remedies this situation somewhat by scaling up this factor by conditioning on two words, and the model given in the paper’s next section completely eliminates this objection by specifying a theory predicting phrasal-level local coherences of an arbitrary length.

1.1. Methods
1.1.1. Data
This experiment makes use of the Dundee corpus (Kennedy and Pynte 2005) of eye-movement data from 10 participants reading 51,000 words each of The Independent (a British newspaper). To get part-of-speech tags for the corpus, we parsed it using the Charniak parser (Charniak 2000). From the eye-tracking record given in the corpus, we calculated our dependent measure of first pass times for each word, defined as the total duration of all fixations on a word prior to having fixated anything to its right.

1.1.2. Model
We tested the local coherence factor in a linear mixed-effect model (Pinheiro and Bates 2000; for a psycholinguistic introduction see also Baayen, Davidson, and Bates 2008) of the first pass times on each word, containing 11 fixed effect control factors and participant as a random effect, as in Demberg and Keller (2008). Coefficient estimates and significance levels were estimated by Markov chain Monte Carlo (MCMC) sampling (Baayen, Davidson, and Bates 2008).

1.1.3. Control Variables
We took our control factors from Demberg and Keller (2008). They included linguistic properties such as word length in characters, the logarithm of word frequency per million as estimated from the British National Corpus (BNC), bigram probability ($P(w_{i-1}|w_i)$; also estimated from the BNC), and position in the sen-
tence in words. In addition, they included lexicalized and unlexicalized syntactic surprisal ($-\log P(w_i | w_{i-1})$), as well as eye movement properties such as the landing position with respect to the word, the number of characters between last fixation and current fixation, and whether the previous word was fixated.

### 1.1.4. Factor Estimation
For each word-tag pair in the Dundee corpus, we estimated $P(t_i | w_i)$ from a Charniak-parsed version of the BNC. We used two versions of the factor: $P_m$ was the maximum likelihood estimate (MLE) and $P_s$ was a smoothed version. $P_s$ was calculated by smoothing the MLE with a type-averaged distribution over part-of-speech tags. Specifically, a type-averaged distribution $P_{pr}$ was calculated for a given tag $t_i$ as

$$
P_{pr}(t_i) = \frac{\sum_{w} P_m(t_i | w)}{|w|}
$$

where $w$ ranges over word types (as opposed to tokens). The smoothed probability $P_s$ of a tag $t_i$ given a word $w_i$ is then calculated to be

$$
P_s(t_i | w_i) = \frac{c(t_i, w_i) + \beta(P_{pr}(t_i))}{c(w_i) + \beta}
$$

where $c(t_i, w_i)$ returns the count of $w_i$ tagged as $t_i$ in the corpus, and $\beta$ is set to minimize Dundee corpus perplexity.

### 1.1.5. Log Transform
In addition to the probabilities themselves, the base-2 logarithms of both versions of the factor, $P_m$ and $P_s$, were also entered into the regression.

### 1.1.6. Data Selection
We excluded from the analysis any word in the Dundee corpus that had punctuation, contained numbers, did not contain letters, occurred as the first or last word of a line, or that did not occur in the BNC. In addition, we excluded the first-pass times on any word which had a first-pass time of zero.

### 1.2. Results
The better fit to the data was achieved by the log-transformed versions of the factor. The log $P_m$ factor had a coefficient estimate of -0.71 ($p < .0001$), and the log $P_s$ factor had a coefficient estimate of -0.80 ($p < .01$). By contrast, the linear fit version of $P_m$ had an insignificant coefficient estimate of -0.84 ($p = .42$), and $P_s$ had a coefficient estimate of -2.31 ($p < .05$). To better visualize the results, a natural spline regression was performed on $P_s$ with 11 equally spaced knots. The result is shown in Figure 1 with bootstrapped 95% confidence intervals.
1.3. Discussion
Since the better fit was achieved using the logarithmic version of the factors, we focus here on their interpretation. For both $P_m$ and $P_s$, doubling the probability of a tag reduces the first-pass time by about 7 or 8 tenths of a millisecond. Looking at the spline regression in Figure 1 reveals that most of the differences it is accounting for exist for probabilities under 0.2. While this seems to be a somewhat small effect, the significance levels of these factors reveal that the effects are reliable. This provides the first evidence for the effects of local coherences (albeit local coherences consisting of one word) in the reading of naturalistic text.

2. Experiment 2
The second experiment is very similar to the first. In this case, however, we test for effects of two-word local coherences, again at the part-of-speech tag level, using as our factor an estimate of $P(t_i|w_{i-1})$. To see how this factor is a measure of two-word local coherences, consider again the definition of local coherence effects we used above: a string of words $w$ that out of context would suggest one very likely parse which is impossible (or at least highly unlikely) in context. If we again invert that definition, because part-of-speech tags are mutually exclusive, we see that local coherence effects occur when the only possible part-of-speech tag for a word in a sentential context is highly unlikely out of that context. Once again, we are using the actual part-of-speech tag of a word as a crude estimate of the only possible part-of-speech tag.

Take as an example a two-word sequence from Tabor, Galantucci, and Richardson, player tossed. Out of context this string is likely to have a parse where tossed is a past tense verb and very unlikely to have a parse where tossed is a past participle. Thus, this factor would predict reading tossed as a past participle to be especially difficult given that the previous word was player. Dynamical systems theories such
as Tabor and Hutchins (2004) would also predict a word to be read more slowly as the $P(t_i|w_{i-1}^i)$ decreases, since the lexically-anchored tree fragments for the two words should cooperate to cause a large amount of interference to the globally correct parse. While Gibson’s theory would not predict the previous word to have an effect, this model still looks very similar to the sort of integration process he proposes, and may be one natural way to scale his theory up to the multi-word case.

2.1. Methods

2.1.1. Data, Model, and Control Variables
The data, model, and control variables used for Experiment 2 are the same as for Experiment 1.

2.1.2. Factor Estimation
For each word-word-tag triplet in the Dundee corpus, we estimated $P(t_i|w_{i-1}^i)$ from the Charniak-parsed BNC. As in Experiment 1, we used two versions of the factor: $P_m$ was the maximum likelihood estimate (MLE) and $P_s$ was version smoothed from the MLE using the same method as in Experiment 1.

2.1.3. Log Transform
As before, the base-2 logarithms of $P_m$ and $P_s$ were also entered into the regression.

2.1.4. Data Selection
As in Experiment 1, we excluded from the analysis any word in the Dundee corpus that had punctuation, contained numbers, did not contain letters, or occurred as the first or last word of a line. Words were also excluded when the bigram of that word and the previous word did not occur in the BNC. In addition, as in Experiment 1, we excluded the first-pass times on any word which had a first-pass time of zero.

2.2. Results
As in Experiment 1, the better fit to the data was achieved by the log-transformed versions of the factors. The $\log P_m$ factor had a coefficient estimate of -0.43 ($p < .0001$), and the $\log P_s$ factor had a coefficient estimate of -4.10 ($p < .0001$). The linear fit version of $P_m$ had a coefficient estimate of -2.94 ($p < .05$), and $P_s$ had a coefficient estimate of -17.56 ($p < .0001$). As before, a natural spline regression performed on $P_s$ is shown in Figure 2 with bootstrapped confidence intervals.

2.3. Discussion
Inspecting the coefficients for the better-fitting logarithmic versions of the factor reveals that this factor has a much larger effect that of Experiment 1. The coefficient estimate for the smoothed version indicates that doubling the probability of a tag reduces first-pass time by only about 4 tenths of a millisecond. The reason that this coefficient is even smaller than in Experiment 1 is probably simply because the probability function we are estimating is much more sparse than before, and thus smoothing is necessary. The coefficient estimate for the smoothed version of the factor indicates that doubling the probability of a tag reduces the first-pass time.
3. The Model

The demonstration in Experiment 2 that the effects of multi-word local coherences appear in the reading of naturalistic text underscores the need for a theory of phrasal-level local coherences which can make broad-coverage predictions. This section presents one such model. The basic intuition behind it is that incrementally processing a sentence can be conceptualized as a process of updating one’s beliefs. Such an analogy has been used to motivate surprisal-based theories of sentence processing (Hale 2001; Levy 2008), where beliefs about the structure of a sentence after seeing the first \( i - 1 \) words in the sentence \( w_{i-1} \) are updated upon encountering \( w_i \). In this case, the surprisal of a word \((- \log P(w_i|w_{i-1})\)) is equivalent to the Kullback-Leibler divergence of the beliefs after \( w_i \) from the beliefs before (Levy 2008). Our model focuses on another belief-update process in sentence processing: updating beliefs about the structures that a string of words is likely to have independent of context to beliefs about what structures it is likely to have in context.

A bit more formally, it views the process of integrating a string of words \( w_j \) into a sentence as beginning with a ‘bottom-up’ prior distribution of syntactic structures likely to span \( w_j \) and integrating that with ‘top-down’ knowledge from the previous words in the sentence \( w_{i-1} \) in order to reach a posterior distribution conditioning on \( w_j \) over which structures actually can span \( w_j \). This belief update process can be viewed as a rational reconstruction of the Tabor and Hutchins (Tabor and
Klinton Bicknell, Roger Levy, and Vera Demberg

Hutchins (2004) model, where – instead of the system dynamics of competition between arbitrary tree fragments – differences between prior and posterior probability distributions over syntactic structures determine processing difficulty.

More formally still, when integrating \( w^j_i \) into a sentence, for each syntactic category \( X \), we can define the prior probability conditioned only on \( w^j_i \) that \( w^j_i \) will form the beginning of that category, i.e., that an \( X \) exists which begins at index \( i \) and spans at least through \( j \):

\[
(6) \quad \text{Prior: } P(X^k \geq j | w^j_i)
\]

It is important to note here that this prior probability is conditional only on the value of \( w^j_i \) and not the values of \( i \) or \( j \); that is, in the prior probability, \( i \) and \( j \) should be interpreted merely as a way to coindex the start and end points of the string of words being integrated with a category \( X \) potentially spanning them, and not as making reference to position in the full sentence string.

For each category \( X \), this prior probability will be updated to the posterior probability of that category spanning \( w^j_i \) given all the words seen so far:

\[
(7) \quad \text{Posterior: } P(X^k_i \geq j | w^j_i)
\]

In the equation for the posterior, of course, the indices \( i \) and \( j \) are positions in the sentence string, and not merely coindices.

Given these prior and posterior beliefs, we predict difficulty to arise in cases where the prior requires substantial modification to reach the posterior, that is, cases in which the prior and posterior make substantially different predictions for categories. A strong local coherence will have sharply different prior and posterior distributions, causing difficulty. We measure \( M_{ij} \), the amount of modification required, as the K-L divergence of the prior from the posterior summed over syntactic categories. That is, if \( N \) is the set of non-terminal categories in the grammar, the size of the belief update is modeled as

\[
(8) \quad M_{ij} \overset{\text{def}}{=} \sum_{X \in N} D\left( P(X^k_i \geq j | w^j_i) \| P(X^k_i \geq j | w^j_i) \right)
\]

In Bicknell and Levy (2009), we show how to compute \( M_{ij} \) by using Bayesian inference on quantities calculated in ordinary probabilistic incremental Earley parsing with a stochastic context-free grammar (SCFG). Furthermore, we present the results of a computational experiment showing that our model makes the correct predictions on the original local coherences experiment of Tabor, Galantucci, and Richardson (2004).

4. Conclusion

This paper has made two contributions to the study of local coherences: a set of corpus experiments and a new model. The two novel corpus experiments showed evidence that effects of local coherences consisting of one or two words occur in the reading of naturalistic text. The first experiment showed a reliable effect of single-
Correcting the Incorrect

word local coherences, such as those predicted by the model of Gibson (2006), and compatible with dynamical systems models such as that of Tabor and Hutchins (2004). The second experiment showed an even larger effect of two-word local coherences, such as those predicted by dynamical systems models such as Tabor and Hutchins (2004). Such results give ecological validity to the study of local coherences and demonstrate that they are not merely artifacts in the processing of very rare sentence types. Furthermore, the results suggested that two-word local coherences appear to be stronger than single-word coherences.

This latter observation led to the description of a mathematical model predicting where effects of local coherences will occur in arbitrary sentences. The fundamental insight of this model is that effects of local coherences can be described in terms of updating prior beliefs about the structures a new string of words is likely to take independent of context into posterior beliefs about what structures it is likely to take given contextual information. This model predicts local coherence effects to occur whenever prior and posterior beliefs are substantially different.

In contrast to Gibson’s model, this model can account for all existing results on phrasal-level local coherences. In contrast to the dynamical systems models, it does not require assuming a rather arbitrary parsing mechanism with a large number of free parameters, but rather is described in terms only of probabilities in a grammar (which can be estimated in a principled and straightforward way). Future work will test that model’s predictions on the reading of naturalistic text in a similar way to Experiments 1 and 2.

Acknowledgments
This work has benefited from useful discussion with Nathaniel Smith and from feedback from audiences at the the 2008 annual CUNY Conference on Human Sentence Processing and the 2009 Annual Meeting of the LSA. The research was supported by NIH Training Grant T32-DC000041 from the Center for Research in Language at UC San Diego to the first author.

References

