

Socially Optimal Coordination: Characterization and Policy Implications*

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Abstract

In recent years there has been a growing interest in macro models with heterogeneity in information and complementarity in actions. These models deliver promising positive properties, such as heightened inertia and volatility. But they also raise important normative questions, such as whether the heightened inertia and volatility are socially undesirable, whether there is room for policies that correct the way agents use information in equilibrium, and what are the welfare effects of the information disseminated by the media or policy makers. We argue that a key to answering all these questions is the relation between the equilibrium and the socially optimal degrees of coordination. The former summarizes the private value from aligning individual decisions, whereas the latter summarizes the value that society assigns to such an alignment once all externalities are internalized.

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1 Introduction

In recent years, there has been a growing interest in models that share the following two key features: (i) heterogeneity in information about the underlying economic fundamentals; and (ii) complementarity in actions. Examples include the beauty-contest game in Morris and Shin (2002); the investment games in Angeletos and Pavan (2004) and Angeletos, Lorenzoni and Pavan (2006); the common-interest game in the paper by Morris and Shin in this issue; and the business-cycle models in Woodford (2002), Hellwig (2005), Lorenzoni (2005), and Roca (2005).¹

These models deliver interesting *positive* properties, such as *inertia* (i.e., slow response to changes in the underlying fundamentals) and heightened *non-fundamental volatility* (i.e., high sensitivity to common noise in information about the underlying fundamentals). But they also raise important *normative* questions.

1. Is the heightened inertia or volatility due to complementarity socially undesirable?
2. Are there policies that could manipulate the way agents use information, and thereby correct the sensitivity of the equilibrium to both fundamentals and noise? If yes, how do these policies look like?
3. How does the incompleteness of information affect welfare? What is the social value of the information disseminated by prices, market experts, or the media? Should central banks disclose the information they collect and the forecasts they make about the economy in a transparent and timely fashion, or is there room for “constructive ambiguity”?

To answer these questions, one needs: (1) to compare the equilibrium use of information with an appropriate constrained efficiency benchmark, namely the use of available information that maximizes welfare; (2) to identify policies that implement the efficient use of information as an equilibrium; and (3) to understand the comparative statics of equilibrium welfare with respect to the information structure.

Ongoing work (Angeletos and Pavan, 2006a,b) undertakes these tasks in a broad class of economies with heterogeneous information, externalities,

¹This class of models differs from global games in that the coordination element is moderate enough that the equilibrium is unique no matter the precision of private and public information. Related are also models with “inattentive” agents, as in the paper by Mankiw and Reis in this issue.

and strategic complementarity or substitutability in actions, and discusses a variety of applications. In this paper, we restrict attention to a (sub)class in which inefficiency emerges *only* when information is incomplete, thus isolating the inefficiencies that originate in the use of information from other possible distortions.

This facilitates the main message of this paper: the key to answering all the questions above is the relation between the equilibrium and the socially optimal degrees of coordination. The former is identified with the slope of an agent's best response with respect to others' activity, and pins down the equilibrium use of information; the latter is identified with the slope that would make agents internalize all externalities, and pins down the efficient use of information. The former summarizes the private value from aligning individual decisions; the latter summarizes the value that society assigns to such an alignment.

2 A simple model

There is a continuum of agents, indexed by i and uniformly distributed over $[0, 1]$, each choosing an action $k_i \in \mathbb{R}$ (e.g., think of k as investment). There is also a government, which makes transfers t_i to the agents, subject to budget balance, $\int t_i di = 0$.

Payoffs. Agent i 's payoff is $u_i + t_i$, where

$$u_i = -(k_i - \theta)^2 - r(L_i - \bar{L}) - r^*\bar{L}.$$

$\theta \in \mathbb{R}$ is an exogenous random fundamental (e.g., aggregate productivity), $L_i = \int (k_j - k_i)^2 dj$ is the mean-square distance of i 's action from other agents' actions, $\bar{L} = \int L_i di$ is the average of these distances, and r and r^* are non-negative scalars.

This payoff structure has a simple interpretation. The term $(k_i - \theta)^2$ captures the value of taking an action that is aligned with the fundamentals, whereas the term L_i introduces a private value to aligning one's action to those of others—the source of strategic complementarity. The term \bar{L} , on the other hand, introduces an externality which controls the discrepancy, if any, between the private and the social value of such alignment.

Indeed, since \bar{L} does not depend on agent i 's action, from a *strategic* viewpoint it is as if payoffs were $u_i^{private} = -(k_i - \theta)^2 - rL_i$. Aggregate welfare, on the other hand, is given by

$$w \equiv \int u_i di = \int [-(k_i - \theta)^2 - r^*L_i] di.$$

Hence, from a *social* perspective it is as if payoffs were given by $u_i^{social} = -(k_i - \theta)^2 - r^* L_i$. In this sense, r parametrizes the private value of aligning choices, while r^* parametrizes the social value of such alignment.

Remark. While the particular payoffs assumed here admit a convenient interpretation, the key assumption is only that inefficiency vanishes once information is complete (Angeletos and Pavan, 2006a,b). Here, the complete-information equilibrium and the first-best allocation are both given by $k_i = \theta$ for all i .

Information. Before agents move, nature draws θ from a Normal distribution with mean μ and variance σ_θ^2 . The realization of θ is not observed by the agents. Instead, agents observe private signals $x_i = \theta + \xi_i$ and a public signal $y = \theta + \varepsilon$, where ξ^i and ε are, respectively, idiosyncratic and common Normal noises, independent of one another as well as of θ , with variances σ_x^2 and σ_y^2 .

3 Equilibrium degree of coordination

We start by characterizing equilibrium without government intervention ($t_i = 0$ for all i); we reintroduce the government in Section 5.

The best response of agent i solves $\partial \mathbb{E}_i u_i / \partial k_i = 0$, which reduces to

$$k_i = (1 - \alpha) \mathbb{E}_i \theta + \alpha \mathbb{E}_i K \tag{1}$$

where $\alpha = r / (1 + r)$ and $K = \int k_j dj$.² The equilibrium is then given by the fixed point to this best-response condition.

The slope of best responses with respect to aggregate activity K , which here is a simple increasing function of r , captures how much agents care to align their actions with one another; it summarizes how the private value to coordination impacts equilibrium behavior. We accordingly call α the *equilibrium degree of coordination*.

This coefficient plays a key role on how agents use information in equilibrium. When $\alpha = 0$, condition (1) reduces to $k_i = \mathbb{E}_i \theta = \lambda_\mu \mu + \lambda_y y + \lambda_x x_i$, where $(\lambda_\mu, \lambda_y, \lambda_x)$ are the familiar Bayesian weights.³ That is, when $\alpha = 0$, the equilibrium action is simply the best predictor of θ . When instead $\alpha > 0$, the equilibrium is given by the linear strategy

$$k_i = \gamma_\mu \mu + \gamma_y y + \gamma_x x_i,$$

²For any random variable z , we let $\mathbb{E}_i z \equiv \mathbb{E}_i [z | x_i, y]$.

³ $\lambda_\mu \equiv \sigma_\theta^{-2} / \sigma^{-2}$, $\lambda_y \equiv \sigma_y^{-2} / \sigma^{-2}$, and $\lambda_x \equiv \sigma_x^{-2} / \sigma^{-2}$, where $\sigma^{-2} \equiv \sigma_\theta^{-2} + \sigma_y^{-2} + \sigma_x^{-2}$.

where the coefficients $(\gamma_\mu, \gamma_y, \gamma_x)$ are given by

$$\gamma_\mu = \frac{\lambda_\mu}{1 - \alpha\lambda_x} > \lambda_\mu, \quad \gamma_y = \frac{\lambda_y}{1 - \alpha\lambda_x} > \lambda_y, \quad \gamma_x = \frac{(1 - \alpha)\lambda_x}{1 - \alpha\lambda_x} < \lambda_x.$$

That is, a positive degree of coordination increases the reliance of equilibrium actions to the prior and to public information, and decreases the reliance to private information.

The logic for this result is simple. The prior and the public signal are relatively better predictors of others' activity than the private signal. The higher α , the more agents care to align their choices, and hence the more they find it optimal to rely on μ and y . It follows that both γ_μ and γ_y increase with α , whereas γ_x decreases with α .

The equilibrium use of information in turn determines how aggregate activity responds to both fundamentals and noise. Using $\gamma_\mu + \gamma_x + \gamma_y = 1$ and $y = \theta + \varepsilon$, we can write aggregate activity as $K = \gamma_\mu\mu + (1 - \gamma_\mu)\theta + \gamma_y\varepsilon$, where ε is common noise. It follows that a higher α , by increasing γ_μ and γ_y , reduces the sensitivity of aggregate activity to the fundamental and increases its sensitivity to common noise. That is, a higher degree of coordination increases both *inertia* and *volatility*. At the same time, because a higher α reduces the reliance on private information, and hence the sensitivity to idiosyncratic noise, it also reduces the *dispersion* of activity in the cross-section of the population.

4 Socially optimal degree of coordination

We next turn to the characterization of a particular constrained efficient allocation. This allocation is the strategy that maximizes ex-ante welfare (i.e., expected utility behind the veil of ignorance) taking as given the dispersion of information in the population. It can be represented as the solution to a planner's problem, where the planner can perfectly control how each agent uses his available information, but can not transfer information from one agent to another.

As it turns out, the efficient allocation is the strategy that satisfies

$$k_i = (1 - \alpha^*)\mathbb{E}_i\theta + \alpha^*\mathbb{E}_iK, \quad (2)$$

where $\alpha^* = 2r^*/(1 + 2r^*)$. Condition (2) is the analog of (1) with α^* replacing α . This suggests a simple interpretation of condition (2). The efficient allocation can be implemented by manipulating the equilibrium degree of coordination perceived by the agents (for example, through taxes,

as we will see in the next section). The coefficient α^* then summarizes how much the planner wants the agents to align their actions. We accordingly identify α^* with the *(socially) optimal degree of coordination*.

Just as α pins down the equilibrium use of information, α^* pins down the efficient use of information: the efficient allocation is given by

$$k_i = \gamma_\mu^* \mu + \gamma_y^* y + \gamma_x^* x_i,$$

where the coefficients $(\gamma_\mu^*, \gamma_y^*, \gamma_x^*)$ are as in (3) replacing α with α^* . By implication, the discrepancy, if any, between the equilibrium and the efficient use of information is determined merely by the discrepancy, if any, between α and α^* : the sensitivity of the equilibrium allocation to the prior mean and to public information is inefficiently high if and only if $\alpha > \alpha^*$. The answer to the first question raised in the introduction thus reduces to a simple comparison between α and α^* .

Result 1. *If $\alpha > \alpha^*$, then the inertia and the volatility featured in equilibrium are inefficiently high; welfare would be higher if agents were to perceive a lower complementarity in their actions. But if $\alpha \leq \alpha^*$, then the heightened levels of inertia and volatility featured in equilibrium are anything but excessive.*

5 Optimal policy

When the equilibrium use of information is inefficient ($\alpha \neq \alpha^*$), a novel role for policy emerges: welfare can be enhanced with policies that manipulate the agents' incentives to align their decisions. In our framework, this can be achieved with a relatively simple linear tax system, which is the incomplete-information analogue of a Pigou tax system—the key is to make the tax rate contingent on ex-post aggregate activity.

Consider the following tax scheme. Transfers take place at the end of the game, once agents have made their choices; at that point, the government either observes θ directly, or it infers it by observing K and y . The transfer made to agent i is then given by

$$t_i = -\tau(K, \theta) k_i + T(K, \theta),$$

where $\tau(K, \theta)$ is the marginal tax rate and $T(K, \theta)$ a lump-sum transfer. The tax rate is given by $\tau(K, \theta) = (2 + 2r)(\tau_K K + \tau_\theta \theta)$, for some $\tau_K, \tau_\theta \in \mathbb{R}$; the coefficients τ_K and τ_θ parametrize the sensitivity of the tax rate to

aggregate activity and to the fundamental, while the term $2 + 2r$ is just a normalization. Finally, budget balance imposes $T(K, \theta) = \tau(K, \theta)K$.

Agent i anticipates that the tax rate he will pay per unit of k_i will depend on aggregate activity K . His best response is thus given by

$$k_i = (1 - \alpha - \tau_\theta) \mathbb{E}_i \theta + (\alpha - \tau_K) \mathbb{E}_i K.$$

It follows that the proposed policy implements the efficient allocation as an equilibrium if and only if $\tau_K = \alpha - \alpha^* = -\tau_\theta$. Hence, the optimal contingency of τ on K is dictated by the difference between α and α^* .

Result 2. *Any inefficiency in the inertia or volatility of the equilibrium allocation can be corrected by appropriately designing the contingency of the marginal tax rate on aggregate activity. The optimal tax rate must increase with K if and only if $\alpha > \alpha^*$.*

6 Social value of information

We now show how the relation between α and α^* helps understand the comparative statics of equilibrium welfare with respect to information.⁴

We find it useful to decompose any change in the information structure into an *accuracy* and a *commonality* effect. We identify the accuracy of available information with the reciprocal of the total noise in the agents' forecasts of the fundamental, and its commonality with the correlation of noise across agents.⁵

Welfare is lower under incomplete than under complete information because the noise in the agents' information induces "errors" in their actions relative to what they would have done if they knew θ . These errors manifest themselves in two dimensions. First, common noise (i.e., noise in public information) generates non-fundamental volatility, that is, variation in aggregate activity K relative to the complete-information level θ . Second, idiosyncratic noise (i.e., noise in private information) generates cross-sectional dispersion, that is, variation in individual activity k across agents. Both types of errors contribute to lower welfare.

⁴We focus on equilibrium without government. Since the optimal policy restores any efficiency in the equilibrium use of information, the welfare effects of information in an economy with optimal policy coincide with those in an economy where $\alpha = \alpha^*$.

⁵That is, letting $\omega_i \equiv \theta - \mathbb{E}_i \theta$ denote agent i 's forecast error, we define accuracy as $\sigma^{-2} = 1/\text{Var}(\omega_i)$ and commonality as $\delta = \text{Corr}(\omega_i, \omega_j)$, for $i \neq j$. It is easy to check that $\sigma^{-2} = \sigma_\theta^{-2} + \sigma_y^{-2} + \sigma_x^{-2}$, while $\delta = (\sigma_\theta^{-2} + \sigma_y^{-2}) / \sigma^{-2}$.

An increase in accuracy for given commonality—a reduction in total noise for given composition of noise—reduces both types of errors and hence necessarily increases welfare. An increase in commonality for given accuracy, on the other hand, substitutes one type of error for another: in equilibrium it decreases dispersion but can increase volatility. Whether this increases welfare depends again on the relation between α and α^* .

Result 3. (i) *Equilibrium welfare necessarily increases with the accuracy of information.* (ii) *If $\alpha \leq \alpha^*$, welfare also increases with commonality; if instead $\alpha > \alpha^*$, welfare is non-monotonic in commonality.*

To understand part (ii), note that, when the planner chooses the optimal degree of coordination, he effectively faces a trade off between dispersion and volatility: the higher the degree of coordination perceived by the agents, the lower the sensitivity to idiosyncratic noise and the higher the sensitivity to common noise, and hence the lower the dispersion and the higher the volatility. It follows that the optimal degree of coordination reflects social preferences over dispersion and volatility: a higher α^* means a higher willingness to substitute dispersion for volatility.

When the equilibrium use of information is efficient ($\alpha = \alpha^*$), higher commonality, by substituting dispersion for volatility, necessarily raises welfare (provided $\alpha^* > 0$, so that there is a strictly positive value to aligning choices). When, instead, the equilibrium use of information is inefficient ($\alpha \neq \alpha^*$), the welfare effect of commonality depends on its effect on this inefficiency. Intuitively, an increase in commonality always facilitates a closer alignment of decisions, but whether this improves efficiency depends on whether there is too little or too much alignment to start with. When $\alpha < \alpha^*$, higher commonality mitigates the inefficiency and therefore necessarily raises welfare. When instead $\alpha > \alpha^*$, higher commonality exacerbates the inefficiency and may thereby reduce welfare.

Having understood the social value of accuracy and commonality, it is now easy to understand the welfare effects of any change in information. For example, suppose that a prompt release of news by the media, more transparency in central-bank communications, or more timely publication of macroeconomic statistics by the administration, result in an increase in the precision of available public information, keeping constant the precision of private information. This induces an increase in both the accuracy and the commonality of information. By Result 3, the increase in accuracy necessarily boosts welfare; but the increase in commonality can decrease welfare if the equilibrium degree of coordination is inefficiently high. The following is then an immediate implication.

Result 3b. *More precise public information necessarily increases welfare if $\alpha \leq \alpha^*$, but can decrease welfare if α is sufficiently higher than α^* .*

As another example of how the relation between α and α^* affects the social value of information, suppose that a policy maker faces the choice between two possible ways of communicating to the market: very fine messages that convey a lot of information but—precisely because they are *too* fine—are likely to be interpreted in idiosyncratic ways; and simpler messages that convey less information but—precisely because they are simpler—admit a common interpretation. Then, the policy maker effectively faces a trade-off between accuracy and commonality; if $\alpha^* \geq \alpha$, so that commonality is socially desirable, he may well opt for the coarser messages. (See the paper by Morris and Shin in this issue for a motivation and further implications.)

7 Conclusion

We argued that the relation between the private and the social value to coordination is the key to answering all the normative questions raised in the introduction—whether the inertia and volatility featured in equilibrium are inefficient, what is the role of policy in correcting how agents use information, and what is the social value of information.

We illustrated this point within the context of a specific example, which admitted a simple parametrization of the private and social values of coordination. In general, the mapping from the payoff structure to the equilibrium and optimal degrees of coordination need not be as simple as in the example considered here. Yet, the main insight extends: the private value of aligning choices can be read from the slope of best responses, while the social value of such alignment can be read from the slope of best responses that would make agents internalize all externalities. (See Angeletos and Pavan, 2006a.)

For example, in the beauty-contest models of Morris and Shin (2002) and Angeletos, Lorenzoni and Pavan (2006), the complementarity perceived by the agents is not warranted from a social perspective ($\alpha > 0$ but $\alpha^* = 0$). This explains why in these models welfare may decrease with higher commonality, and hence may also decrease with more precise public information. In contrast, in the business-cycle models of Hellwig (2005) and Roca (2005), the social value of coordination turns out to be higher than the private one ($\alpha^* > \alpha$). This is because individual utility falls with cross-sectional dispersion in prices—an externality that raises the social

value of aligning prices across firms. As a result, the heightened inertia and volatility featured in these models due to the complementarity in pricing decisions are anything but excessive; and welfare necessarily increases with more precise public information.

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