# Wall Street and Silicon Valley: A Delicate Interaction

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## Motivation

- "Technological revolutions and financial bubbles seem to go hand in hand"— The Economist, September 21, 2000
- Arrival of new, unfamiliar, investment opportunities
  - "Internet craze" late 1990s
  - "biotech revolution" early 1980s
  - "new financial instruments" mid 2000s

 $\Rightarrow$  high uncertainty, abnormal real and financial activity (Pastor and Veronesi, 2009)

- Financial markets look at real sector for clues and vice versa
  - co-movements in real investment and financial prices
- Do such co-movements reflect efficient response to available information?
- Or could they be product of excessive waves of optimism and pessimism?

# This Paper

- Positive and normative implications of information spillovers between real and financial sector?
- Information spillovers from financial mkts to real economy
  - quite well studied
- Information spillovers from real to financial sector
  - largely under-explored
- Source of non-fundamental volatility
  - dampen response to fundamental shocks
  - amplify response to noise and higher-order-uncertainty
- Symptoms of (constrained) inefficiency
  - policy interventions
- Mechanism: collective signaling (from real to financial sector)
  - source of endogenous complementarities
  - micro-foundation for "beauty-contests" and "irrational-exuberance"

Model

#### 2 Equilibrium

- Ositive Analysis
- Welfare Analysis
- Olicy
- O Robustness and Extensions

# Model

- Two types of agents:
  - entrepreneurs
  - financial investors
- Two project phases:
  - **start-up**: entrepreneurs decide whether to start new project of unknown profitability
  - IPO stage: entrepreneurs expand project using IPO proceeds

## Model: Technology

- Starting a project (*t* = 1)
  - 1 unit of perishable good
- Subsequent expansion (t = 2)
  - $k \in \mathbb{R}_+$ : period-2 expansion
- Output at t = 3:

$$q = \Theta k^{\alpha}$$

Θ: underlying fundamental

## Model: Timing

- At t = 1, each entrepreneur endowed with 1 unit of perishable good
  - consume  $(n_i = 0)$
  - invest to start project  $(n_i = 1)$
- At t = 2, profile  $(n_i)_{i \in [0,1]}$  of start-up activity publicly observed
- Entrepreneurs who did not initiate project at t = 1
  - no other source of income
  - no further action
- Entrepreneurs who initiated project
  - receive no income at t = 2
  - finance project expansion  $k_i$  by selling shares in IPO mkt
  - Budget constraint

$$k_i = p_i s_i$$

- At t = 3, fundamental  $\Theta$  publicly revealed
  - Entrepreneurs receive  $(1 s_i) \Theta k_i^{\alpha}$
  - Investors receive  $s_i \Theta k_i^{\alpha}$

## Model: Information

• 
$$\theta \equiv \log \Theta$$
 with  $\theta \sim \mathcal{N}\left(0, \pi_{\theta}^{-1}\right)$ 

- Entrepreneurs observe  $x_i = \theta + \xi_i, \quad \xi_i \sim \mathcal{N}\left(0, \pi_x^{-1}\right)$  $y = \theta + \varepsilon, \quad \varepsilon \sim \mathcal{N}\left(0, \pi_y^{-1}\right)$
- "Representative" investor observes
   w = θ + η, with η ∼ N (0, π<sub>ω</sub><sup>-1</sup>)
- Investor's information at beginning of t = 2: I = {ω, (n<sub>j</sub>)<sub>j∈[0,1]</sub>}
- Entrepreneur *i*'s information at beginning of  $t = 2: \mathcal{J}_i = \{x_i, y, (n_j)_{j \in [0,1]}\}$
- Market-generated information: M ≡ (p<sub>i</sub>, s<sub>i</sub>, k<sub>i</sub>)<sub>i∈[0,N]</sub>

## Model: Financial Market Microstructure

- Similar to Kyle (1985)
- Each entrepreneur *i* submits supply correspondence

$$S_i^s((\tilde{p}_j)_{j\in[0,N]}, (\tilde{k}_j)_{j\in[0,N]\setminus i}|\mathcal{J}_i)$$

Representative investor submits demand correspondences (S<sup>d</sup><sub>i</sub>(·|𝒯))<sub>i∈[0,N]</sub>, one for each active IPO i ∈ [0, N], with each

$$S^d_i((\widetilde{p}_j)_{j\in[0,N]},(\widetilde{k}_j)_{j\in[0,N]}|\mathcal{I})$$

- Auctioneer selects triples (*p<sub>i</sub>*, *s<sub>i</sub>*, *k<sub>i</sub>*)<sub>*i*∈[0,*N*]</sub> so that
  - each mkt clears
  - each expansion funded with IPO proceeds  $(k_i = p_i \cdot s_i)$
- Two differences wrt Kyle (1985):
  - endogenous dividend (depends on k<sub>i</sub>)
  - entrepreneurs do not have mkt power

## Model: Payoffs

• Entrepreneurs' lifetime utility:  $U_i = c_{i1} + \beta c_{i2} + \beta^2 c_{i3}$ ,

• 
$$c_{i1} = 1 - n_i$$

- $c_{i2} = 0$
- $c_{i3} = 0$  if  $n_i = 0$  and  $c_{i3} = (1 s_i)\Theta k_i^{\alpha}$  otherwise.
- At t = 2, representative investor can produce consumption good out of labor, /, at one-to-one rate
  - perfectly elastic supply of external funds
- Consumption levels of representative investor

$$c_2 = I - \int_{i \in [0,N]} p_i s_i di$$
 and  $c_3 = \int_{i \in [0,N]} s_i \Theta k_i^{\alpha} di$ ,

Investor's lifetime utility:

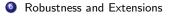
$$V = \int_{i \in [0,N]} \left[ \beta \Theta k_i^{\alpha} - p_i \right] s_i di$$

Model

#### 2 Equilibrium

- Ositive Analysis
- Welfare Analysis

#### Olicy



Equilibrium

• PBE satisfying following restrictions/refinements:

- *p<sub>i</sub>* depends only on mkt information (standard)
- representative investor's posterior about  $\theta$  is normal with mean  $\hat{\theta} \equiv \mathbb{E}[\theta|\mathcal{I}]$ normally distributed (known variances)
- Each entrepreneur "informationally small"
  - investor's posterior about aggregate TFP  $\theta$  invariant to  $(n_i, p_i, s_i, k_i)$
  - ...function of cross-sectional distribution  $(n_j, p_j, s_j, k_j)_{j \in [0, N]}$

• Representative investor's demand in IPO mkt i perfectly elastic at

$$p = \beta \hat{\Theta} k^{\alpha}$$

where

$$\hat{\Theta} \equiv \mathbb{E}[\Theta | \mathcal{I}'] \quad \textit{and} \quad \mathcal{I}' = \{\omega, (n_j)_{j \in [0,1]}\} \cup \{(p_j, s_j, k_j)_{j \in [0,N]}\}$$

# Equilibrium: IPO Stage

- "Relaxed" problem in which entrepreneur i can condition his supply on  $\hat{\Theta}$
- For every  $\hat{\Theta}$ , entrepreneur chooses (p, s, k) that maximize his utility s.t.

• 
$$k = p \cdot s$$
  
•  $p = \beta \hat{\Theta} k^{\alpha}$ 

• To invest k, entrepreneur must sell

$$s = \frac{k}{\beta \hat{\Theta} k^{lpha}}$$

• Entrepreneur's payoff

$$(1-s)\Theta k^{lpha}=rac{\Theta}{eta\hat{\Theta}}\left[eta\hat{\Theta}k^{lpha}-k
ight]$$

thus maximized by

$$K(\hat{\Theta}) = (\alpha \beta \hat{\Theta})^{\frac{1}{1-\alpha}}, \qquad P(\hat{\Theta}) = \alpha^{\frac{\alpha}{1-\alpha}} (\beta \hat{\Theta})^{\frac{1}{1-\alpha}}, \qquad S(\hat{\Theta}) = \alpha$$

 Because p = P(Θ̂) is invertible, solution to relaxed problem can be implemented by submitting supply schedule

$$S_i^s((p_j)_{j\in[0,N]},(k_j)_{j\in[0,N]\setminus i}|\mathcal{J}_i)=K(P^{-1}(p_i))/p_i.$$

 Because each (p<sub>i</sub>, s<sub>i</sub>, k<sub>i</sub>) depends only on Ô, representative investor does not update his beliefs about Θ after observing mkt outcomes:

$$\hat{\Theta} \equiv \mathbb{E}[\Theta | \mathcal{I}'] = \mathbb{E}[\Theta | \mathcal{I}].$$

 Remark: same conclusions if each entrepreneur submits mkt order instead of limit order

## Equilibrium: Start-up Stage

• Each entrepreneur *i* finds it optimal to start project iff

$$\beta^2 \mathbb{E}_i[(1-s_i)\Theta k_i^{\alpha}] \geq 1$$

• Using normality of 
$$\hat{\theta} \equiv \mathbb{E}[\theta | \mathcal{I}']$$
 and of  $\theta | \mathcal{I}$ ,  
 $n_i = 1 \quad \Leftrightarrow \quad (1 - \alpha) \mathbb{E}_i[\theta] + \alpha \mathbb{E}_i[\hat{\theta}] \ge C$ 

#### • First direction of feedback mechanism:

• higher 
$$\hat{ heta} \Rightarrow$$
 higher IPO price  $\Rightarrow$  higher startup activity, N

### Equilibrium: Market valuation

Using Normality

$$n_i = 1 \quad \Leftrightarrow \quad (1-b)x_i + by \geq c$$

Aggregate level of startup activity:

$$\mathsf{N} = \mathsf{Pr}\left((1-b)x_i + by \ge c | \, heta, y
ight) = \Phi\left(\sqrt{\pi_x} rac{(1-b) heta + by - c}{1-b}
ight)$$

• Observation of N conveys same information as "endogenous" signal

$$z \equiv (1-b) heta + by = heta + barepsilon$$
  
 $\pi_z = \pi_y/b^2$ 

- Investors cannot tell apart whether high N driven by high  $\theta$  or correlated error,  $\varepsilon$ , in entrepreneurs' beliefs
- Hence,

$$\hat{\boldsymbol{\Theta}} = \mathbb{E}[\boldsymbol{\Theta} | \mathcal{I}'] = \mathbb{E}[\boldsymbol{\Theta} | \boldsymbol{\omega}, \boldsymbol{N}] = \mathbb{E}[\boldsymbol{\Theta} | \boldsymbol{\omega}, \boldsymbol{z}]$$

- Second direction of feedback mechanism:
  - higher startup activity  $N \Rightarrow$  higher  $\hat{\Theta} \Rightarrow$  higher IPO prices

## Equilibrium: Fixed Point

Using

$$\hat{\theta} = \mathbb{E}[\theta|\omega, z] = \frac{\pi_{\omega}}{\pi}\omega + \frac{\pi_{z}}{\pi}z,$$
$$\mathbb{E}_{i}[\hat{\theta}] = \frac{\pi_{\omega} + \pi_{z}(1-b)}{\pi}\mathbb{E}_{i}[\theta] + \frac{\pi_{z}}{\pi}by$$

where

$$\mathbb{E}_i[\theta] = \delta_x x_i + \delta_y y$$

with

$$\delta_x \equiv \frac{\pi_x}{\pi_{ heta} + \pi_x + \pi_y}$$
 and  $\delta_y \equiv \frac{\pi_y}{\pi_{ heta} + \pi_x + \pi_y}$ 

• Hence, each entrepreneur finds it optimal to start project iff

$$(1-b')x_i+b'y\geq c'$$

• There exist functions  $\Gamma : \mathbb{R} \to \mathbb{R}$  and  $\Lambda : \mathbb{R} \to \mathbb{R}$  s.t. if  $b^*$  is fixed point of  $\Gamma$  and  $c^* = \Lambda(b^*)$ , then there exists eq. in which each entrepreneur starts a project iff

$$(1-b^*)x_i+b^*y\geq c^*$$

#### Proposition 1

(i) There always exists eq. in which  $b^* \in (0, 1)$ . (iii) Such eq. unique for all  $\alpha \leq \bar{\alpha}$ . (iv) For  $\alpha > \bar{\alpha}$ , multiple equilibria

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# **Positive Analysis**

## Role of information spillovers

- Suppose investors do not learn from N
- $\hat{\theta}$  is linear function of exogenous signal  $\omega=\theta+\eta$
- Since entrepreneurs do not possess any information about  $\eta$ ,  $\mathbb{E}_i[\hat{\theta}]$  is linear transformation of  $\mathbb{E}_i[\theta]$
- In this case,

$$n_i = 1 \quad \Leftrightarrow \quad \mathbb{E}_i[ heta] \geq \hat{C}$$

Equivalently,

$$n_i = 1 \quad \Leftrightarrow \quad (1 - \delta)x_i + \delta y \geq \hat{c}$$

where

$$\delta_x \equiv rac{\pi_x}{\pi_ heta + \pi_x + \pi_y}$$
 and  $\delta_y \equiv rac{\pi_y}{\pi_ heta + \pi_x + \pi_y}$ 

• With information spillovers:  $b^* > \delta$ 

#### Proposition 2

Informational spillovers from real to financial sector amplify contribution of noise to aggregate volatility:

$$\frac{\partial N/\partial \varepsilon}{\partial N/\partial \theta} = b^* > \delta$$

## Mispricing and speculation

• Entrepreneurs' startup rule:

$$n_i = 1 \quad \Leftrightarrow \quad \mathbb{E}_i[\theta] + \alpha \mathbb{E}_i[\hat{\theta} - \theta] \ge C$$

#### • Mispricing:

$$\hat{\theta} - \theta = rac{\pi_\omega}{\pi} \eta + rac{\pi_z}{\pi} b^* arepsilon$$

- Higher  $p \Rightarrow$  lower cost of capital  $\Rightarrow$  higher return to startup activity
- Reminiscent of dot-com bubble: when entrepreneurs expect financial mkt to "overvalue" their businesses ⇒ higher startup activity (Pastor and Veronesi, 2009)

$$\mathbb{E}_i[\varepsilon] = y - \mathbb{E}_i[\theta] = (1 - \delta_y)y - \delta_x x$$

- Because higher y contributes to both higher E<sub>i</sub>[θ] and higher E<sub>i</sub>[θ̂ θ], relative sensitivity of startup activity to sources with correlated noise higher than what warranted by informativeness of such sources
- Spillover from entrepreneurs' collective optimism to exuberance in financial mkt crowds out private information and amplifies non-fundamental volatility

#### Proposition 3

In eq., each entrepreneur starts project iff

$$\mathbb{E}_i[(1-r)\theta + r\Phi^{-1}(N)] \ge c^{\#}$$

- binary-action coordination game among entrepreneurs
- Similar to "beauty-contest" literature but here strategic complementarity endogenous
  - each entrepreneur cares about other entrepreneurs' decisions because aggregate startup activity signals higher profitability and hence leads to higher IPO prices
  - complementarity originates in
    - collective signaling from Silicon Valley to Wall Street

#### Proposition 4

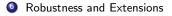
As long as eq. is unique ( $\alpha < \bar{\alpha}$ ), higher  $\alpha$  implies higher contribution of correlated noise to aggregate volatility.

- Higher  $\alpha$ : higher sensitivity of IPO prices to mkt beliefs
- Sectors with high growth potential and high finance dependence most prone to "irrational exuberance", "manias" and "panics"
  - especially true in early stages, when significant uncertainty about eventual profitability

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# Welfare Analysis

## Efficiency

- Are above properties symptom of inefficiency?
- Welfare:

$$\int_0^1 \left\{ n_i \left( \beta^2 \Theta k_i^\alpha - \beta k_i \right) + (1 - n_i) \right\} di = 1 + N \left( \beta^2 \Theta k^\alpha - \beta k - 1 \right)$$

where  $N = \int n_i di$  (concavity:  $k_i = k$  all i)

Restricting attention to linear rules

$$n_i = 1 \quad \Leftrightarrow \quad (1-b)x_i + by \geq c,$$

planner's problem:

$$\max_{\substack{(b,c)\in\mathbb{R}^{2},\mathcal{K}\in\mathsf{C}}} \mathbb{E}\left[N(z)\left(\beta^{2}\Theta\mathcal{K}(\omega,z)^{\alpha}-\beta\mathcal{K}(\omega,z)-1\right)\right]$$
  
s.t.  $z=\theta+b\varepsilon$ ,  $N(z)=\Phi\left(\frac{\sqrt{\pi_{x}}}{1-b}(z-c)\right)$ 

where  $\boldsymbol{\mathsf{C}} \equiv \{\mathcal{K}: \mathbb{R}^2 \to \mathbb{R}\}$ 

• Efficiency in period-2 expansions:

$$\mathcal{K}(\omega, z) = rg\max_k \left\{eta \hat{\Theta} k^lpha - k
ight\},$$

where  $\hat{\Theta} = \mathbb{E}[\Theta|\omega, z]$ 

- Same condition as under mkt equilibrium
- Equilibrium expansions thus efficient conditional on available information

$$\mathcal{K}(\omega, z) = \mathcal{K}(\hat{\Theta}) = (\alpha \beta \hat{\Theta})^{\frac{1}{1-\alpha}}$$

• ...yet available information need not be efficient

## Efficiency

### Proposition 5

Efficiency in startup decisions

$$n_i = 1 \quad \Leftrightarrow \quad (1-b^\diamond) x_i + b^\diamond y \geq c^\diamond$$

requires lower sensitivity to correlated noise:

 $b^\diamond < b^*$ 

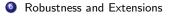
- Eq. contribution of correlated noise to aggregate volatility inefficiently high
- Two reasons why  $b^\diamond < b^*$ :
  - speculative startup activity not warranted
  - information externality: reducing *b* increases precision of endogenous signal *z* and hence efficiency of period-2 expansions
- Both inefficiencies originate in information spillover
- Additional inefficiency in "levels":  $c^{\diamond} \neq c^{*}$ 
  - akin to holdup problem
    - private return from starting project:  $eta^2(1-lpha)\Theta K^lpha$
    - social return:  $\beta^2 \Theta K^{\alpha} \beta K$

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#### Selection 1



Policy

- Proportional tax  $T(\Pi, p)$  on entrepreneurs' profits contingent on IPO price
- Planner can infer  $(\Theta, \hat{\Theta})$  from P and  $\Pi$ 
  - hence, de facto, T contingent  $(\Theta, \hat{\Theta})$
- Net-of-taxes return to start-up activity:

$$(1 - T(\Theta, \hat{\Theta})) \Pi(\Theta, \hat{\Theta})$$

can be manipulated so as to implement efficient allocations

#### • Tax $\tau(p)$ on financial trades

- cost to investors of buying shares: (1+ au) ps
- $\tau$  increasing in p (macro-prudential)

• Because 
$$p = P(\hat{\Theta})$$
, de facto,  $\tau = T(\hat{\Theta})$ 

Equilibrium prices:

$$p = \frac{\beta \hat{\Theta} f(k)}{1 + T(\hat{\Theta})}$$

- Such policies improve efficiency of entrepreneurs' entry decisions, but distorts stage-2 investment
  - cannot implement efficient allocations but can improve over laissez-faire eq.

- Cap on shares entrepreneurs can sell
  - can increase sensitivity of start-up activity to fundamentals
  - forcing entrepreneurs to retain more "skin in the game" reduces speculative motive

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# Robustness and Extensions

### Robustness

"Irrational exuberance"

- correlated bias in beliefs
- 2 correlated taste for startup activity
- Imperfectly correlated fundamentals \Operation;
- Imperfectly elastic demand schedules
  - risk averse traders
- Q Richer signals Wall Street receives from Silicon Valley sales and orders
- Sicher entrepreneurs' signals
- Endogenous collection of entrepreneurs' information

- Waves of startup activity and IPOs
  - later entrepreneurs learn from earlier ones
- Short-termism driven by managerial compensation
  - alternative mechanism for real sector to care about asset prices

- Implications of information spillovers from real to financial sector
  - amplification and non-fundamental volatility
  - bubbly co-movements in real investment and asset prices
  - inefficiency in startup activity
- Corrective policies:
  - taxes on profits contingent on IPO prices
  - taxes on financial trades
  - IPO regulations caps on shares sold

**THANKS!** 

#### Definition 1

Eq. consists of startup strategies  $n_i(x_i, y)$ , supply correspondences  $S_i^s(\cdot)$ , demand correspondences  $S_i^d(\cdot)$ , IPO prices  $(p_i)_{i \in [0,N]}$ , investment expansions  $(k_i)_{i \in [0,N]}$ , shares issuances  $(s_i)_{i \in [0,M]}$ , and beliefs,  $\mu$  jointly satisfying: (i) for all  $(x_i, y)$ ,

$$n_i\left(x_i,y
ight)\inrg\max_k\mathbb{E}\left[ \left|1-n_i+n_ieta^2\left((1-s_i)\Theta k_i^lpha
ight)
ight| \left|x_i,y
ight|
ight];$$

(ii) for all *J<sub>i</sub>*, all (*p̃<sub>j</sub>*)<sub>*j*∈[0,*M*]</sub>, (*k̃<sub>j</sub>*)<sub>*j*∈[0,*M*]\*i*</sub>, *S<sup>s</sup><sub>i</sub>*(·) maximizes Π<sub>*i*</sub> = (1 − *s<sub>i</sub>*)Θ*k<sub>i</sub><sup>α</sup>*; given entrepreneurs' posterior beliefs about Θ, constraint *k<sub>i</sub>* = *s<sub>i</sub>p<sub>i</sub>*, and others' limit orders;
(iii) for all *I*, (*S<sup>d</sup><sub>i</sub>*(·))<sub>*i*∈[0,*M*]</sub> maximizes *V* = *f* [βΘ*f*(*k<sub>i</sub>*) − *p<sub>i</sub>*] *s<sub>i</sub>di* given investor's posterior beliefs, constraint *k<sub>i</sub>* = *s<sub>i</sub>p<sub>i</sub>*, and others' limit orders;
(iv) each active market *i* ∈ [0, *M*] clears and *k<sub>i</sub>* = *s<sub>i</sub>p<sub>i</sub>*;
(v) beliefs are consistent with Bayes' rule on path.

