Simple New Keynesian Model without Capital

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What's It Good For?

- Conveying basic principles of macroeconomics -
 - Concept and measurement of *output gap*:
 - 'difference between the actual economy and where would be if policy was managed as well as possible'.
 - Importance of aggregate demand.
 - problems when it goes awry.
 - Important policy objective: assuring the right level of aggregate demand.
- Thinking through the operating characteristics of policy rules:
 - Inflation targeting, Tax/spending rules, Leverage restrictions on banks.
- Can even use it to learn econometrics
 - how well do standard econometric estimators work?
 - how good is HP filter at estimating output gap?

Our Approach to NK Model

- We will derive the familiar 'three equation NK model', but they will not be our starting point.
 - Start with households, firms, technology, etc....
- Necessary to build the model from scratch -
 - need this to uncover the principles hiding inside it
 - needed to know how to 'go back to the drawing board' and modify the model so it can address interesting questions:
 - how should macro prudential policy be conducted?
 - how might currency mismatch problems affect the usual transmission of exchange rate depreciation to the economy?
 - what should the role of inflation, labor markets, credit growth, stock markets, etc., be in monetary policy?
 - how does an expansion of unemployment benefits in a recession affect the business cycle?

Households

• Problem:

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left(\log C_t - \exp(\tau_t) \frac{N_t^{1+\varphi}}{1+\varphi} \right), \ \tau_t = \lambda \tau_{t-1} + \varepsilon_t^{\tau}$$

s.t. $P_t C_t + B_{t+1} \le W_t N_t + R_{t-1} B_t + \text{Profits net of taxes}_t$

• First order conditions:

$$\frac{1}{C_t} = \beta E_t \frac{1}{C_{t+1}} \frac{R_t}{\bar{\pi}_{t+1}}$$
(5)
$$\exp(\tau_t) C_t N_t^{\varphi} = \frac{W_t}{P_t}.$$

Goods Production

• A homogeneous final good is produced using the following (Dixit-Stiglitz) production function:

$$Y_t = \left[\int_0^1 Y_{i,t}^{\frac{\varepsilon-1}{\varepsilon}} dj\right]^{\frac{\varepsilon}{\varepsilon-1}}$$

• Each intermediate good, $Y_{i,t}$, is produced as follows:

$$Y_{i,t} = \overbrace{A_t}^{=\exp(a_t)} N_{i,t}, \ a_t = \rho a_{t-1} + \varepsilon_t^a$$

• Before discussing the firms that operate these production functions, we briefly investigate the socially efficient ('First Best') allocation of labor across i, for given N_t :

$$N_t = \int_0^1 N_{it} di$$

Efficient Sectoral Allocation of Labor

- With Dixit-Stiglitz final good production function, there is a socially optimal allocation of resources to all the intermediate activities, $Y_{i,t}$
 - It is optimal to run them all at the same rate, *i.e.*, $Y_{i,t} = Y_{j,t}$ for all $i, j \in [0, 1]$.
- For given N_t , it is optimal to set $N_{i,t} = N_{j,t}$ for all $i, j \in [0, 1]$
- In this case, final output is given by

$$Y_t = e^{a_t} N_t.$$

- Best way to see this is to suppose that labor is *not* allocated equally to all activities.
 - But, this can happen in a million different ways when there is a continuum of inputs!
 - Explore one simple deviation from $N_{i,t} = N_{j,t}$ for all $i, j \in [0, 1]$.

Suppose Labor Not Allocated Equally

• Example:

$$N_{it} = \begin{cases} 2\alpha N_t & i \in \left[0, \frac{1}{2}\right] \\ 2(1-\alpha)N_t & i \in \left[\frac{1}{2}, 1\right] \end{cases}, \ 0 \le \alpha \le 1.$$

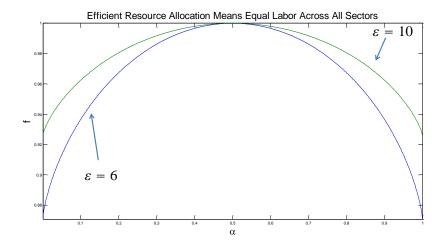
 Note that this is a particular distribution of labor across activities:

$$\int_{0}^{1} N_{it} di = \frac{1}{2} 2\alpha N_{t} + \frac{1}{2} 2(1-\alpha) N_{t} = N_{t}$$

Labor Not Allocated Equally, cnt'd

$$\begin{split} Y_{t} &= \left[\int_{0}^{1} Y_{i,t}^{\frac{s-1}{\varepsilon}} di\right]^{\frac{s}{\varepsilon-1}} \\ &= \left[\int_{0}^{\frac{1}{2}} Y_{i,t}^{\frac{s-1}{\varepsilon}} di + \int_{\frac{1}{2}}^{1} Y_{i,t}^{\frac{s-1}{\varepsilon}} di\right]^{\frac{s}{\varepsilon-1}} \\ &= e^{a_{t}} \left[\int_{0}^{\frac{1}{2}} N_{i,t}^{\frac{s-1}{\varepsilon}} di + \int_{\frac{1}{2}}^{1} N_{i,t}^{\frac{s-1}{\varepsilon}} di\right]^{\frac{s}{\varepsilon-1}} \\ &= e^{a_{t}} \left[\int_{0}^{\frac{1}{2}} (2\alpha N_{t})^{\frac{s-1}{\varepsilon}} di + \int_{\frac{1}{2}}^{1} (2(1-\alpha)N_{t})^{\frac{s-1}{\varepsilon}} di\right]^{\frac{s}{\varepsilon-1}} \\ &= e^{a_{t}} N_{t} \left[\int_{0}^{\frac{1}{2}} (2\alpha)^{\frac{s-1}{\varepsilon}} di + \int_{\frac{1}{2}}^{1} (2(1-\alpha))^{\frac{s-1}{\varepsilon}} di\right]^{\frac{s}{\varepsilon-1}} \\ &= e^{a_{t}} N_{t} \left[\int_{0}^{\frac{1}{2}} (2\alpha)^{\frac{s-1}{\varepsilon}} + \frac{1}{2} (2(1-\alpha))^{\frac{s-1}{\varepsilon}} \right]^{\frac{s}{\varepsilon-1}} \\ &= e^{a_{t}} N_{t} \left[\frac{1}{2} (2\alpha)^{\frac{s-1}{\varepsilon}} + \frac{1}{2} (2(1-\alpha))^{\frac{s-1}{\varepsilon}} \right]^{\frac{s}{\varepsilon-1}} \end{split}$$

$$f(\alpha) = \left[\frac{1}{2}(2\alpha)^{\frac{\varepsilon-1}{\varepsilon}} + \frac{1}{2}(2(1-\alpha))^{\frac{\varepsilon-1}{\varepsilon}}\right]^{\frac{\varepsilon}{\varepsilon-1}}$$



Final Goods Production

- Final good firms:
 - maximize profits:

$$P_t Y_t - \int_0^1 P_{i,t} Y_{i,t} dj,$$

subject to:

$$Y_t = \left[\int_0^1 Y_{i,t}^{\frac{\varepsilon-1}{\varepsilon}} dj\right]^{\frac{\varepsilon}{\varepsilon-1}}$$

•

– Foncs:

$$Y_{i,t} = Y_t \left(\frac{P_t}{P_{i,t}}\right)^{\varepsilon} \to P_t = \left(\int_0^1 P_{i,t}^{(1-\varepsilon)} di\right)^{\frac{1}{1-\varepsilon}}$$

Intermediate Goods Production

• Demand curve for *i*th monopolist:

$$Y_{i,t} = Y_t \left(\frac{P_t}{P_{i,t}}\right)^{\varepsilon}$$

• Production function:

$$Y_{i,t} = \exp(a_t) N_{i,t}, \ \Delta a_t = \rho \Delta a_{t-1} + \varepsilon_t^a$$

• Calvo Price-Setting Friction:

$$P_{i,t} = \left\{ \begin{array}{ll} \tilde{P}_t & \text{ with probability } 1-\theta \\ P_{i,t-1} & \text{ with probability } \theta \end{array} \right.$$

• Real marginal cost:

 $s_{t} = \frac{\frac{d\text{Cost}}{d\text{worker}}}{\frac{d\text{output}}{d\text{worker}}} = \frac{\overbrace{(1-\nu)}^{\text{minimize monopoly distortion by setting} = \frac{\varepsilon-1}{\varepsilon}}{e}$

Optimal Price Setting by Intermediate Goods Producers

• Let

$$\tilde{p}_t \equiv \frac{\tilde{P}_t}{P_t}, \ \bar{\pi}_t \equiv \frac{P_t}{P_{t-1}}.$$

• First order condition implied by optimal price setting:

$$\tilde{p}_t = \frac{K_t}{F_t},$$

where

$$K_t = \frac{\varepsilon}{\varepsilon - 1} s_t + \beta \theta E_t \bar{\pi}_{t+1}^{\varepsilon} K_{t+1}(1)$$

$$F_t = 1 + \beta \theta E_t \bar{\pi}_{t+1}^{\varepsilon - 1} F_{t+1}.(2)$$

• Note:

$$K_{t} = \frac{\varepsilon}{\varepsilon - 1} s_{t} + \beta \theta E_{t} \bar{\pi}_{t+1}^{\varepsilon} \frac{\varepsilon}{\varepsilon - 1} s_{t+1} + (\beta \theta)^{2} E_{t} \bar{\pi}_{t+2}^{\varepsilon} \frac{\varepsilon}{\varepsilon - 1} s_{t+2} + \dots$$

Price Equilibrium Conditions

• Cross-price restrictions imply, given the Calvo price-stickiness:

$$P_t = \left[(1-\theta) \tilde{P}_t^{(1-\varepsilon)} + \theta P_{t-1}^{(1-\varepsilon)} \right]^{\frac{1}{1-\varepsilon}}$$

• Dividing latter by P_t and solving for \tilde{p}_t :

$$ilde{p}_t = \left[rac{1- hetaar{\pi}_t^{arepsilon-1}}{1- heta}
ight]^{rac{1}{1-arepsilon}}$$

• Combining with the first order condition for \tilde{p}_t :

$$\frac{K_t}{F_t} = \left[\frac{1-\theta\bar{\pi}_t^{\varepsilon-1}}{1-\theta}\right]^{\frac{1}{1-\varepsilon}}$$
(3)

Aggregate Inputs and Aggregate Output

• Tack Yun argument:

$$Y_{t}^{*} \equiv \int_{0}^{1} Y_{i,t} di \left(= \int_{0}^{1} e^{a_{t}} N_{i,t} di = e^{a_{t}} N_{t} \right)$$

$$\stackrel{\text{demand curve}}{=} \int_{0}^{1} Y_{t} P_{t}^{\varepsilon} P_{i,t}^{-\varepsilon} di = Y_{t} P_{t}^{\varepsilon} \int_{0}^{1} P_{i,t}^{-\varepsilon} di$$

$$\xrightarrow{=} Y_{t}^{*} = \overbrace{\left(\frac{P_{t}^{*}}{P_{t}}\right)^{\varepsilon}}^{\varepsilon} e^{a_{t}} N_{t}$$

$$P_{t}^{*} = [(1-\theta) \tilde{P}_{t}^{-\varepsilon} + \theta P_{t-1}^{-\varepsilon}]^{\frac{1}{-\varepsilon}}$$

$$\rightarrow p_{t}^{*} = \left[(1-\theta) \tilde{p}_{t}^{-\varepsilon} + \theta \frac{\bar{\pi}_{t}^{\varepsilon}}{p_{t-1}^{*}}\right]^{-1}$$

Goods Equilibrium Conditions

• Relationship between aggregate output and aggregate inputs:

$$C_t = p_t^* A_t N_t, (6)$$

where ('Tack Yun distortion')

$$p_t^* = p^* \left(\bar{\pi}_t, p_{t-1}^* \right) \equiv \left[\left(1 - \theta \right) \left(\frac{1 - \theta \bar{\pi}_t^{(\varepsilon - 1)}}{1 - \theta} \right)^{\frac{\varepsilon}{\varepsilon - 1}} + \theta \frac{\bar{\pi}_t^{\varepsilon}}{p_{t-1}^*} \right]^{-1}$$

Tack Yun Distortion: a Closer Look

• Distortion:

$$p_t^* = p^* \left(\bar{\pi}_t, p_{t-1}^* \right) \equiv \left[\left(1 - \theta \right) \left(\frac{1 - \theta \bar{\pi}_t^{(\varepsilon - 1)}}{1 - \theta} \right)^{\frac{\varepsilon}{\varepsilon - 1}} + \theta \frac{\bar{\pi}_t^{\varepsilon}}{p_{t-1}^*} \right]^{-1}$$

- Distortion, p_t^* , increasing function of lagged distortion, p_{t-1}^* . - Current shocks affect current distortion via $\bar{\pi}_t$ only.
- Derivatives:

$$p_{1}^{*} \left(\bar{\pi}_{t}, p_{t-1}^{*} \right) = - (p_{t}^{*})^{2} \varepsilon \theta \bar{\pi}_{t}^{\varepsilon - 2} \left[\frac{\bar{\pi}_{t}}{p_{t-1}^{*}} - \left(\frac{1 - \theta \bar{\pi}_{t}^{(\varepsilon - 1)}}{1 - \theta} \right)^{\frac{1}{\varepsilon - 1}} \right]$$

$$p_{2}^{*} \left(\bar{\pi}_{t}, p_{t-1}^{*} \right) = \left(\frac{p_{t}^{*}}{p_{t-1}^{*}} \right)^{2} \theta \bar{\pi}_{t}^{\varepsilon}.$$

Linear Expansion of Tack Yun Distortion in Undistorted Steady State

• Linearizing about $ar{\pi}_t = ar{\pi}$, $p^*_{t-1} = p^*$:

$$dp_t^* = p_1^*(\bar{\pi}, p^*) \, d\bar{\pi}_t + p_2^*(\bar{\pi}, p^*) \, dp_{t-1}^*,$$

where $dx_t \equiv x_t - x$, for $x_t = p_t^*$, p_{t-1}^* , $\bar{\pi}_t$.

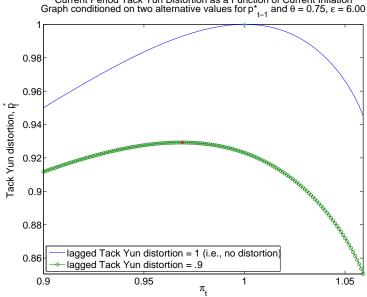
- In an undistorted steady state (i.e., $ar{\pi}_t = p_t^* = p_{t-1}^* = 1)$:

$$p_1^*(1,1) = 0, \ p_2^*(1,1) = \theta.$$

so that

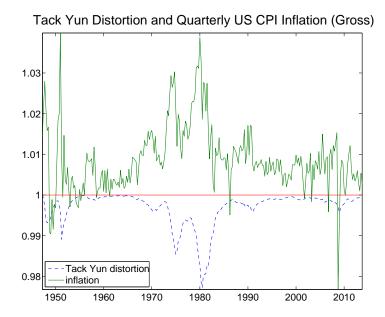
$$egin{array}{rcl} dp_t^* &=& 0 imes dar{\pi}_t + heta dp_{t-1}^* \ & o & p_t^* = 1 - heta + heta p_{t-1}^* \end{array}$$

- Often, people that linearize NK model ignore p_t^* .
 - Reflects that they linearize the model around a price-undistorted steady state.



Current Period Tack Yun Distortion as a Function of Current Inflation

Ignoring Tack Yun Distortion, a Mistake?



First Best Consumption, Employment

- 'First Best Consumption and Employment' useful concepts in simple NK model.
 - Ramsey is the appropriate benchmark, but Ramsey and first best coincide in simple NK model.
- Explained above that with socially efficient sectoral allocation of labor,

$$Y_t = \exp\left(a_t\right) N_t.$$

• First best level of employment and consumption is solution to

$$N_{t}^{\text{best}} = \arg \max_{N} \left\{ \log \left[\exp \left(a_{t} \right) N \right] - \exp \left(\tau_{t} \right) \frac{N^{1+\varphi}}{1+\varphi} \right\}$$

so,

$$N_t^{\text{best}} = \exp\left(-\frac{\tau_t}{1+\varphi}
ight)$$
, $C_t^{\text{best}} = \exp\left(a_t - \frac{\tau_t}{1+\varphi}
ight)$

Linearizing around Efficient Steady State

• In steady state (assuming $\bar{\pi} = 1, 1 - \nu = \frac{\varepsilon - 1}{\varepsilon}$)

$$p^* = 1, \ K = F = rac{1}{1 - eta heta}, \ s = rac{arepsilon - 1}{arepsilon}, \ \Delta a = au = 0, \ N = 1$$

• Linearizing the Tack Yun distortion, (4):

$$p_t^* = 1$$
, t large enough

• Denote the *output gap* in ratio form by X_t :

$$X_t \equiv \frac{C_t}{\exp\left(a_t - \frac{\tau_t}{1 + \varphi}\right)} = p_t^* N_t \exp\left(\frac{\tau_t}{1 + \varphi}\right),$$

where the denominator is the socially efficient ('First Best') level of consumption.

• Then, with $x_t \equiv \hat{X}_t$ and $\hat{p}_t^* = 0$:

$$x_t = \hat{N}_t + rac{d au_t}{1+arphi}$$

NK IS Curve, Baseline Model

• The intertemporal Euler equation, (5), after substituting for C_t in terms of X_t:

$$\frac{1}{X_t \exp\left(a_t - \frac{\tau_t}{1 + \varphi}\right)} = \beta E_t \frac{1}{X_{t+1} \exp\left(a_{t+1} - \frac{\tau_{t+1}}{1 + \varphi}\right)} \frac{R_t}{\bar{\pi}_{t+1}}$$
$$\frac{1}{X_t} = E_t \frac{1}{X_{t+1} R_{t+1}^*} \frac{R_t}{\bar{\pi}_{t+1}},$$

where

value of R_t in 'first best' $\widehat{R_{t+1}^*} \equiv \frac{1}{\beta} \exp\left(a_{t+1} - a_t - \frac{\tau_{t+1} - \tau_t}{1 + \varphi}\right)$ then, (using $\widehat{z_t u_t} = \hat{z}_t + \hat{u}_t$, $\widehat{\left(\frac{u_t}{z_t}\right)} = \hat{u}_t - \hat{z}_t$): $\widehat{X}_t = E_t \left[\widehat{X}_{t+1} - (\widehat{R}_t - \widehat{\pi}_{t+1} - \widehat{R}_{t+1}^*)\right]$

NK IS Curve, Baseline Model

• Note:

$$Z_t = \exp(z_t) \text{, where } z_t \equiv \log Z_t$$
$$\hat{Z}_t \equiv \frac{dZ_t}{Z} = \frac{d\exp(z_t)}{Z} = \frac{Zdz_t}{Z} = dz_t = \log Z_t - \log Z.$$

• Use this to establish, when the steady state is efficient:

$$E_t \left(\hat{R}_t - \hat{\pi}_{t+1} - \hat{R}_{t+1}^* \right) \\ = \log R_t - E_t \pi_{t+1} - E_t \log R_{t+1}^* \\ = r_t - E_t \pi_{t+1} - r_t^*$$

where

$$r_t \equiv \log R_t, \ r_t^* \equiv E_t \log R_{t+1}^*, \ \pi_{t+1} \equiv \log \bar{\pi}_{t+1},$$

• and, in efficient steady state:

$$\log R^* = \log R, \ \log \bar{\pi} = 0.$$

NK IS Curve, Baseline Model

• Substituting

$$\hat{X}_{t} = E_{t} \left[\hat{X}_{t+1} - \left(\hat{R}_{t} - \hat{\bar{\pi}}_{t+1} - \hat{R}_{t+1}^{*} \right) \right], \ x_{t} \equiv \hat{X}_{t},$$

we obtain NK IS curve:

$$x_t = E_t x_{t+1} - E_t \left[r_t - \pi_{t+1} - r_t^* \right]$$

• Also,

$$r_t^* = -\log\left(\beta\right) + E_t \left[a_{t+1} - a_t - \frac{\tau_{t+1} - \tau_t}{1 + \varphi}\right]$$

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Linearized Marginal Cost in Baseline Model

• Marginal cost (using $da_t = a_t$, $d\tau_t = \tau_t$ because $a = \tau = 0$):

$$s_t = (1 - \nu) \frac{\bar{w}_t}{A_t}, \ \bar{w}_t = \exp(\tau_t) N_t^{\varphi} C_t$$
$$\rightarrow \ \hat{w}_t = \tau_t + a_t + (1 + \varphi) \hat{N}_t$$

• Then,

$$\hat{s}_t = \hat{\bar{w}}_t - a_t = (\varphi + 1) \left[\frac{\tau_t}{\varphi + 1} + \hat{N}_t \right] = (\varphi + 1) x_t$$

Linearized Phillips Curve in Baseline Model

• Log-linearize equilibrium conditions, (1)-(3), around steady state:

$$\begin{split} \hat{K}_{t} &= (1 - \beta \theta) \, \hat{s}_{t} + \beta \theta \left(\varepsilon \widehat{\pi}_{t+1} + \hat{K}_{t+1} \right) \, (1) \\ \hat{F}_{t} &= \beta \theta \left(\varepsilon - 1 \right) \widehat{\pi}_{t+1} + \beta \theta \widehat{F}_{t+1} \, (2) \\ \hat{K}_{t} &= \hat{F}_{t} + \frac{\theta}{1 - \theta} \widehat{\pi}_{t} \, (3) \end{split}$$

• Substitute (3) into (1)

$$\hat{F}_t + rac{ heta}{1- heta} \hat{\pi}_t = (1-eta heta) \, \hat{s}_t + eta heta \left(arepsilon \widehat{\pi}_{t+1} + \hat{F}_{t+1} + rac{ heta}{1- heta} \hat{\pi}_{t+1}
ight)$$

• Simplify the latter using (2), to obtain the NK Phillips curve:

$$\pi_t = rac{(1- heta)(1-eta heta)}{ heta} \hat{s}_t + eta \pi_{t+1}$$

Nonlinear Private Sector Equilibrium Conditions

$$K_{t} = \frac{\varepsilon}{\varepsilon - 1} s_{t} + \beta \theta E_{t} \bar{\pi}_{t+1}^{\varepsilon} K_{t+1}(1)$$

$$F_{t} = 1 + \beta \theta E_{t} \bar{\pi}_{t+1}^{\varepsilon - 1} F_{t+1}.(2)$$

$$\frac{K_{t}}{F_{t}} = \left[\frac{1 - \theta \bar{\pi}_{t}^{\varepsilon - 1}}{1 - \theta}\right]^{\frac{1}{1 - \varepsilon}} (3)$$

$$p_{t}^{*} = \left[(1 - \theta) \left(\frac{1 - \theta \bar{\pi}_{t}^{(\varepsilon - 1)}}{1 - \theta}\right)^{\frac{\varepsilon}{\varepsilon - 1}} + \theta \frac{\bar{\pi}_{t}^{\varepsilon}}{p_{t-1}^{*}}\right]^{-1} (4)$$

$$\frac{1}{C_{t}} = \beta E_{t} \frac{1}{C_{t+1}} \frac{R_{t}}{\bar{\pi}_{t+1}} (5)$$

$$C_{t} = p_{t}^{*} A_{t} N_{t}. (6)$$

The Linearized Private Sector Equilibrium Conditions

$$\begin{aligned} x_t &= E_t x_{t+1} - [r_t - E_t \pi_{t+1} - r_t^*] \\ \pi_t &= \frac{(1-\theta)(1-\beta\theta)}{\theta} \hat{s}_t + \beta E_t \pi_{t+1} \\ \hat{s}_t &= (\varphi+1) x_t \\ r_t^* &= -\log(\beta) + E_t \left[a_{t+1} - a_t - \frac{\tau_{t+1} - \tau_t}{1+\varphi} \right] \end{aligned}$$

Monetary policy rule:

$$r_t = \alpha r_{t-1} + (1-\alpha) \left[r + \phi_\pi \pi_t + \phi_x x_t \right]$$

Solving the Model

- Vision about evolution of actual data:
 - Nature draws the exogenous shocks.
 - The economy transforms exogenous shocks into realization of endogenous variables, inflation, output, unemployment, etc.
- 'Solving the model':
 - Determining the model's implications for the mapping from exogenous shocks to endogenous variables.
 - Potentially massive problem: current value of endogenous variables a function of past data and *expected future value of endogenous variables*.
- Primary strategy for solving a model:
 - Find a linear representation ('policy rule') of the endogenous variables, *z_t*, in terms of current and past data only:

$$z_t = A z_{t-1} + B s_t$$

such that the equilibrium conditions (after linearization) are satisfied.

• Exogenous shocks:

$$s_{t} = \begin{pmatrix} \Delta a_{t} \\ \tau_{t} \end{pmatrix} = \begin{bmatrix} \rho & 0 \\ 0 & \lambda \end{bmatrix} \begin{pmatrix} \Delta a_{t-1} \\ \tau_{t-1} \end{pmatrix} + \begin{pmatrix} \varepsilon_{t}^{a} \\ \varepsilon_{t}^{\tau} \end{pmatrix}$$
$$s_{t} = Ps_{t-1} + \epsilon_{t}$$

• Equilibrium Conditions:

• Collecting:

$$E_t \left[\alpha_0 z_{t+1} + \alpha_1 z_t + \alpha_2 z_{t-1} + \beta_0 s_{t+1} + \beta_1 s_t \right] = 0$$

$$s_t - P s_{t-1} - \epsilon_t = 0.$$

• Policy rule:

$$z_t = A z_{t-1} + B s_t$$

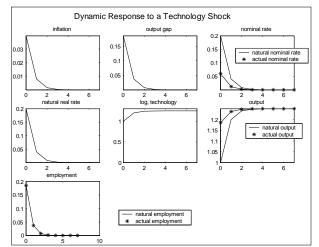
• As before, want A such that

$$\alpha_0 A^2 + \alpha_1 A + \alpha_2 I = 0,$$

• Want *B* such that:

$$(\beta_0 + \alpha_0 B)P + [\beta_1 + (\alpha_0 A + \alpha_1)B] = 0$$

Note: if α = 0, then A = 0 is one solution (there is another one!).



 $\phi_x = 0, \, \phi_\pi = 1.5, \, \beta = 0.99, \, \varphi = 1, \, \rho = 0.2, \, \theta = 0.75, \, \alpha = 0, \, \delta = 0.2, \, \lambda = 0.5.$

