

# Nominal Rigidities and the Dynamic Effects of a Shock to Monetary Policy

by

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# Motivation

- Want to Contribute to Quest for Quantitatively Realistic Model of Monetary Transmission Mechanism.
- Would like to Understand Reasons for Inflation Inertia and Output Persistence.

# A Strategy for Estimating a Monetary Model

- Estimate a ‘Reduced Form’ Model of the Monetary Transmission Mechanism.
- Quantify Notions of ‘Inflation Inertia’ and ‘Output Persistence’.
- Estimate a General Equilibrium Model that is Consistent With Reduced Form.
- *Reality*: In GE, ‘Everything’ Matters - Can’t ‘Split Off’ Monetary Economics, Investment Economics, Labor Economics.
- To Interpret Macro Data, Must Inevitably Think About a Range of Issues:
  - (a) Nominal Frictions:
    - \* Sticky Prices, Wages, etc.
  - (b) Real Features:
    - \* Adjustment Costs in Investment, Variable Capital Utilization, Habit Persistence in Preferences.

# Our Question

- What Nominal Frictions and Real Features are Necessary for a Model to Conform Well with Reduced Form?

## Alternative Strategy for Estimating A Model:

- Compute Unconditional Moments of Data.
- Estimate Model Based on All Moments (Maximum Likelihood).
- Disadvantages of All-Moment Approach:
  - Need to Determine All Shocks in the Model, Not Just Monetary Policy Shocks.
- Advantage of All-Moment Approach.
  - In the End, Want a Model With All Shocks.
- Advantage of Our Limited Information Approach.
  - Can Make Progress Learning About Structure of Economy Without Having to Take a Stand on the Nature of the Non-Monetary Shocks.

# Outline

- (1) Reduced Form Estimate of the Monetary Transmission Mechanism
- (2) The Model
- (3) Assigning Values to Model Parameters
- (4) Empirical Evaluation of Model

# Identification of Monetary Policy Shocks

- Monetary Policy Rule:

$$R_t = \alpha Y_t + \beta P_t + \text{lagged variables} + \varepsilon_t$$

$\varepsilon_t \sim$  Monetary Policy Shock

- Identification Assumptions:

(1)  $\varepsilon_t$  Has No Contemporaneous Effect on  $Y_t, P_t$

(2)  $Y_t, P_t$  Only Variables Observed Contemporaneously

# Identification of Response to Monetary Policy Shocks

- Step 1: Compute  $\varepsilon_t$ , Error Term in Projection of  $R_t$  on  $Y_t$ ,  $P_t$ , lagged variables
- Step 2: Project Economic Variables on Current and Past Values of  $\varepsilon_t$
- Population Projections Estimated Using a VAR Fit to Data.



# VAR Procedure

- VAR variables,  $Z_t$ :

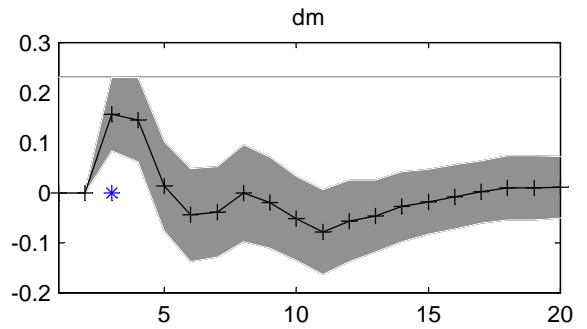
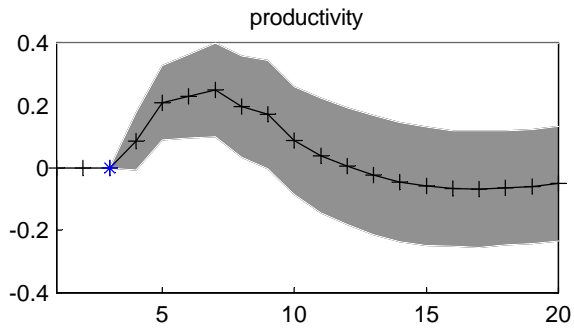
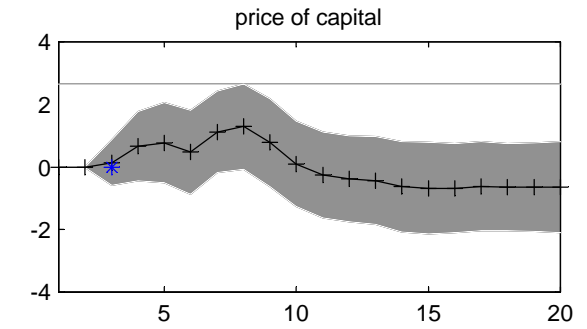
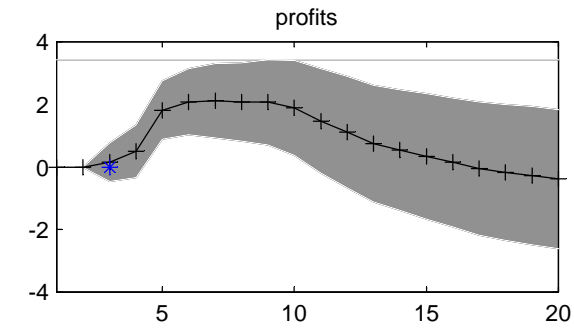
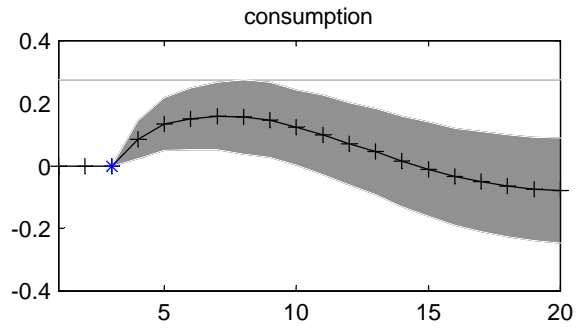
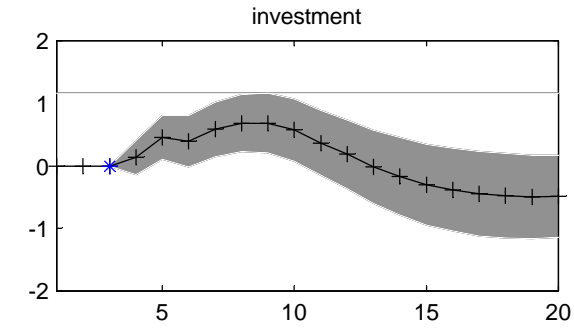
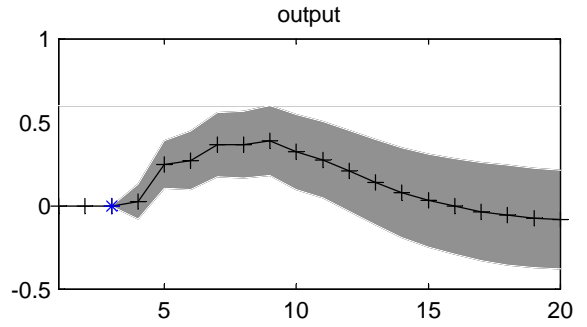
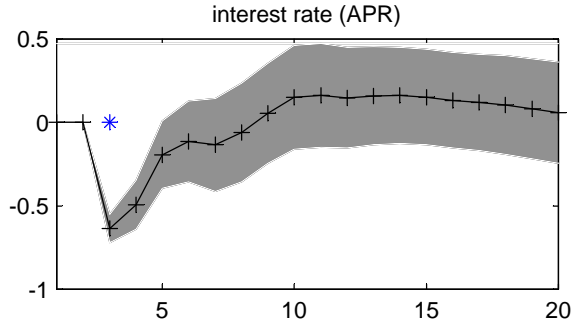
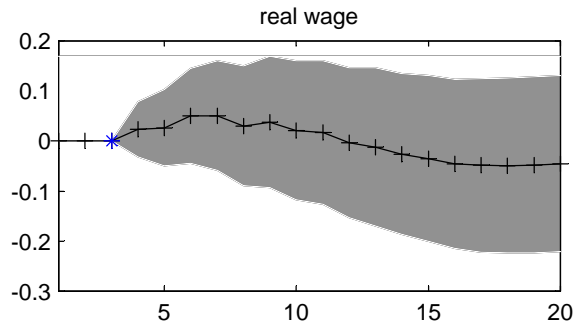
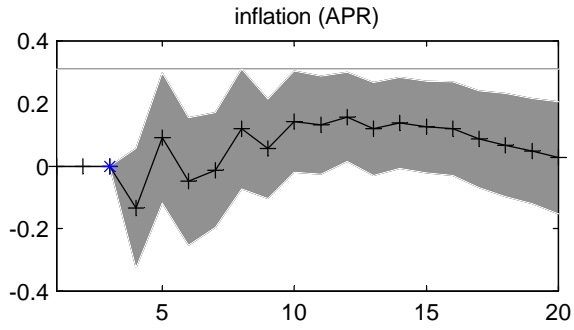
$$Z_t = \begin{pmatrix} \ln(GDP \text{ deflator}) \\ \ln(GDP) \\ \ln(C) \\ \ln(I) \\ \ln(W/P) \\ \ln(\text{Labor Productivity}) \\ \text{Federal Funds Rate} \\ \ln(\text{Profits}) \\ \ln(\text{Price of Capital}) \\ \Delta \ln(M2) \end{pmatrix}$$

- Contemporaneous variables in  $\Omega_t$ : first 6 variables in  $Z_t$ .
- Ordering of First 6, Last Three Irrelevant.
- 4 lag VAR, 1965Q3 - 1995Q3.

# Results of Monetary Policy Shock Analysis

- After a Positive Monetary Shock,  $\varepsilon_t$ :
  - hump-shaped, response of output, consumption, investment with peak effect after about 1.5-2 years.
  - hump-shaped response inflation, with peak response after about 2 years.
  - interest rate down for one year.
  - profits, real wage, labor productivity up.
  - lots of internal propagation!

Estimated VAR Impulse Responses



## Next Step:

- Construct a Model that is Consistent With Identifying Assumptions in Monetary Shock Analysis
- Do Same Projections in the Model as in the Data
- Estimate Combination of Frictions Needed for Outcome of Model and Data Projections to be Quantitatively Similar.

## Findings of Model Analysis:

- Model Does Well at Accounting for Facts
  - Average Duration of Price Contracts:  
Roughly 2 Quarters
  - Average Duration of Wage Contracts:  
Roughly 3.3 Quarters
- Internal Propagation in Model Strong
- Inference is Sensitive to Getting the ‘Real’ Side of the Model Right.
  - Habit Persistence in Preferences.
  - Adjustment Costs in Investment.
  - Variable Capital Utilization.

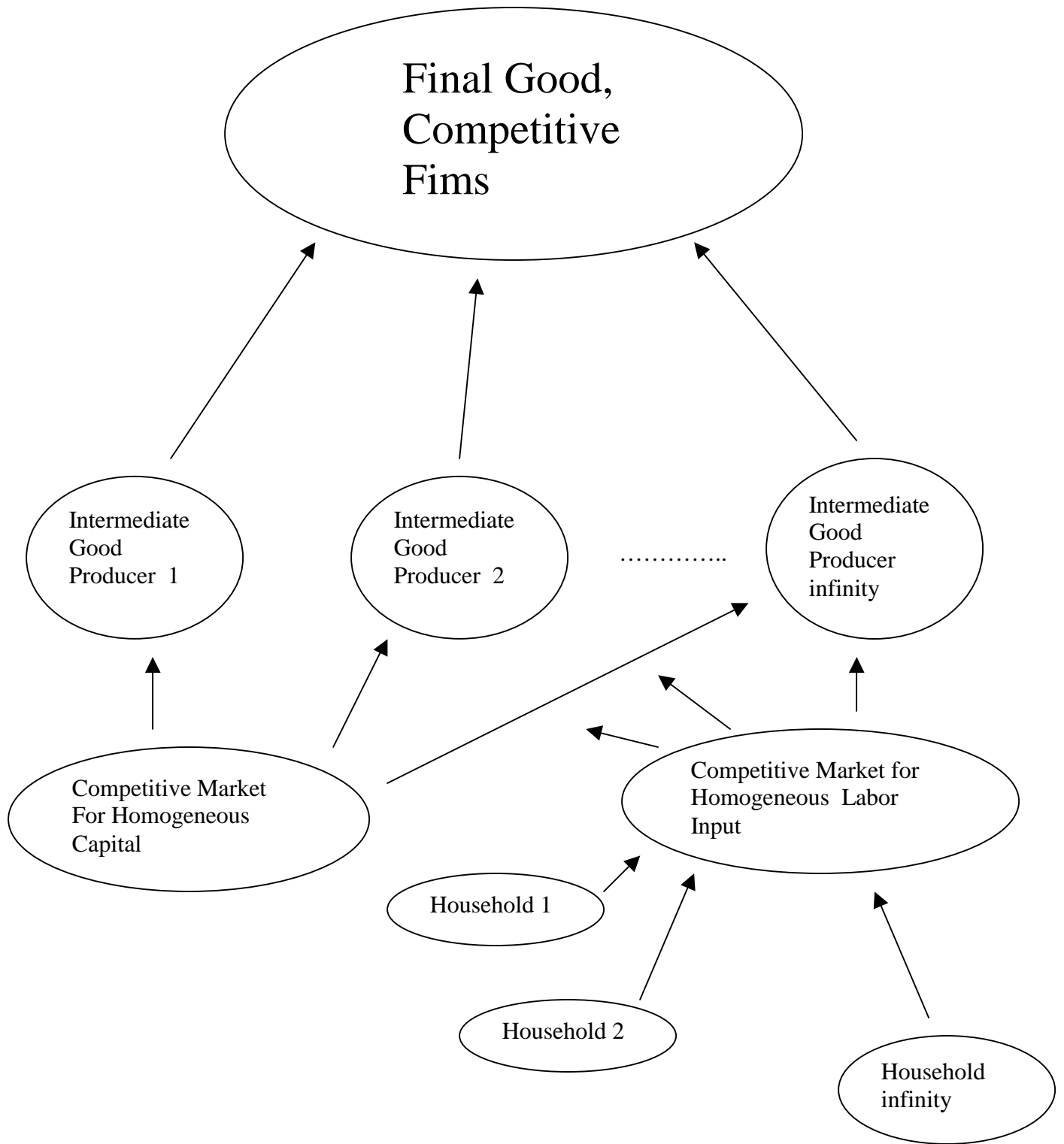
# Model

- Timing Assumptions.
- Firms.
- Households.
- Monetary Authority.

# Timing

- (1) Agents Make Price/Wage Setting, Consumption, Investment, Capital Utilization Decisions.
  - (2) Monetary Policy Shock Realized.
  - (3) Household Money Demand Decision Made.
  - (4) Production, Employment, Purchases Occur, and Markets Clear.
- Note: Wages, Prices and Output Predetermined Relative to Policy Shock.

# Firm Sector





# Firms

## Final Good Firms

- Technology:

$$Y_t = \left[ \int_0^1 Y_{it}^{\frac{1}{\lambda_f}} di \right]^{\lambda_f}, \quad 1 \leq \lambda_f < \infty$$

- Objective:

$$\max P_t Y_t - \int_0^1 P_{it} Y_{it} di$$

- Firms and Prices:

$$\left( \frac{P_t}{P_{it}} \right)^{\frac{\lambda_f}{\lambda_f - 1}} = \frac{Y_{it}}{Y_t}, \quad P_t = \left[ \int_0^1 P_{it}^{\frac{1}{1 - \lambda_f}} di \right]^{(1 - \lambda_f)}.$$

## Intermediate Good Firms -

- Each  $Y_{it}$  Produced by a Monopolist, With Demand Curve:

$$\left( \frac{P_t}{P_{it}} \right)^{\frac{\lambda_f}{\lambda_f - 1}} = \frac{Y_{it}}{Y_t}.$$

- Technology:

$$Y_{it} = K_{it}^\alpha L_{it}^{1-\alpha} - \phi, \quad 0 < \alpha < 1.$$

- Calvo Price Setting:
  - With Probability  $1 - \xi_p$ ,  $i^{th}$  Firm Sets Price,  $P_{it}$ , Optimally, to  $\tilde{P}_t$ .
  - With Probability  $\xi_p$ ,

$$P_{it} = \pi_{t-1} P_{i,t-1}, \quad \pi_t = \frac{P_t}{P_{t-1}}.$$

- Conventional Price-updating:

$$P_{it} = \bar{\pi} P_{i,t-1}.$$

- Firms Setting Prices Optimally at  $t$   
Choose  $\tilde{P}_t$  to max:

$$\begin{aligned}
& v_t [\tilde{P}_t Y_{it} - MC_t Y_{it}] \\
& + \beta \xi_p v_{t+1} [\tilde{P}_t \pi_t Y_{i,t+1} - MC_{t+1} Y_{i,t+1}] \\
& + (\beta \xi_p)^2 v_{t+2} [\tilde{P}_t \pi_t \pi_{t+1} Y_{i,t+2} - MC_{t+2} Y_{i,t+2}] \\
& + \dots
\end{aligned}$$

subject to:

$$\left( \frac{P_t}{\tilde{P}_t} \right)^{\frac{\lambda_f}{\lambda_f - 1}} = \frac{Y_{it}}{Y_t}.$$

$v_t \sim$  value of a dividend at  $t$

$MC_t \sim$  given

- Scaling:

$$\tilde{p}_t = \frac{\tilde{P}_t}{P_t}, \quad w_t = \frac{W_t}{P_t}$$

$$r_t^k = \frac{\text{rental rate on capital}}{P_t}$$

$$s_t = \frac{MC_t}{P_t}.$$

- Real Marginal Cost:

$$s_t = \left( \frac{1}{1-\alpha} \right)^{(1-\alpha)} \left( \frac{1}{\alpha} \right)^\alpha (r_t^k)^\alpha (w_t R_t)^{1-\alpha}$$

- Linear approximation:

$$\hat{x}_t \equiv \frac{x_t - x}{x}.$$

- Approximate (Linearized) Solution:

$$\begin{aligned}\widehat{\tilde{p}}_t &= \hat{s}_t + \sum_{l=1}^{\infty} (\beta\xi_p)^l (\hat{s}_{t+l} - \hat{s}_{t+l-1}) \\ &\quad + \sum_{l=1}^{\infty} (\beta\xi_p)^l (\hat{\pi}_{t+l} - \hat{\pi}_{t+l-1})\end{aligned}$$

- $\hat{s}_{t+l} = \hat{s}_t, \hat{\pi}_{t+l} = \hat{\pi}_t \Rightarrow \widehat{\tilde{p}}_t = \hat{s}_t$

- Aggregate Price Level:

$$\begin{aligned}
 P_t &= \left[ \int_0^1 P_{it}^{\frac{1}{1-\lambda_f}} di \right]^{(1-\lambda_f)} \\
 &= \left[ (1 - \xi_p) \tilde{P}_t^{\frac{1}{1-\lambda_f}} + \xi_p (\pi_{t-1} P_{t-1})^{\frac{1}{1-\lambda_f}} \right]^{1-\lambda_f}
 \end{aligned}$$

- Scale:

$$1 = \left[ (1 - \xi_p) \tilde{p}_t^{\frac{1}{1-\lambda_f}} + \xi_p \left( \frac{\pi_{t-1}}{\pi_t} \right)^{\frac{1}{1-\lambda_f}} \right]^{1-\lambda_f}$$

- Approximately

$$\hat{\tilde{p}}_t = \frac{\xi_p}{1 - \xi_p} [\hat{\pi}_t - \hat{\pi}_{t-1}].$$

- Combining:

$$\hat{\pi}_t = \frac{1}{1 + \beta} \hat{\pi}_{t-1} + \frac{\beta}{1 + \beta} E_{t-1} \hat{\pi}_{t+1} + \frac{(1 - \beta \xi_p)(1 - \xi_p)}{(1 + \beta) \xi_p} E_{t-1} \hat{s}_t,$$

- Or:

$$\hat{\pi}_t = \hat{\pi}_{t-1} + \frac{(1 - \beta \xi_p)(1 - \xi_p)}{\xi_p} E_{t-1} \sum_{j=0}^{\infty} \beta^j \hat{s}_{t+j}$$

- Note: Damped Inflation Response Requires Damped Marginal Cost Response.



- Under Standard Approach to Indexing:

$$\hat{\pi}_t = \beta E_{t-1} \hat{\pi}_{t+1} + \frac{(1 - \beta \xi_p)(1 - \xi_p)}{\xi_p} E_{t-1} \hat{s}_t.$$

- Fuhrer-Moore (1995), Gali-Gertler (1997), Casares-McCallum (2000), Mankiw (2000), Walsh (1998):
  - Standard Approach Fits Data Badly.
  - Need Lagged Inflation.

# Households

- Wage Decision.
- Consumption Decision.
- Investment Decision.
- Capital Utilization Decision.
- Portfolio Decision.

- State Contingent Securities
  - Allow Household to Insulate Consumption, Asset Holdings from Realization of Idiosyncratic Calvo Uncertainty.
  - This Simplifies Computation of Equilibrium.
  - Ignore State Contingent Securities in the Presentation.
  - Households Are Different With Respect to Wages and Employment.

- Preferences:

$$E_{t-1}^h \sum_{l=0}^{\infty} \beta^{l-t} [u(c_{t+l} - bc_{t+l-1}) - z(h_{j,t+l}) + v(q_{t+l})].$$

$b \sim$  habit parameter

$$q = \frac{Q}{P}$$

$$u(\cdot) = \log(\cdot)$$

$$z(\cdot) = \frac{\psi_0}{2} (\cdot)^2$$

$$v(\cdot) = \psi_q \frac{(\cdot)^{1-\sigma_q}}{1-\sigma_q}$$

## Habit Persistence and Response of Consumption

- Recall that After an Expansionary Monetary Policy Shock, we see
  - hump-shaped rise in consumption
  - decline in real interest rate.
- Euler Equation in Standard Model:

$$\frac{u_{c,t}}{\beta u_{c,t+1}} \approx \frac{c_{t+1}}{\beta c_t} = \frac{g_{t+1}}{\beta} = \frac{R_t}{\pi_{t+1}}, \quad \pi_{t+1} = \frac{P_{t+1}}{P_t}.$$

- Problem: Can't Have  $g_t$  High and  $\frac{R_t}{\pi_{t+1}}$  Simultaneously!

- Habit Persistence in Preferences (example):

$u(c_t - b\bar{c}_{t-1})$ ,  $\bar{c}_{t-1} \sim$  aggregate consumption

- Euler Equation:

$$\begin{aligned} \frac{u_{c,t}}{\beta u_{c,t+1}} &\approx \frac{c_{t+1} - bc_t}{\beta (c_t - bc_{t-1})} = \frac{g_{t+1} - b}{\beta \left(1 - \frac{b}{g_t}\right)} \\ &\approx \frac{g_{t+1} - bg_t}{\beta(1 - b)} \end{aligned}$$

- Result:
  - $g_{t+1}$  and  $g_t$  Can Both be High, as Long as  $g_{t+1} < bg_t$ .
  - Consistent with Simultaneous Hump-Shape  $c$  Response and Low Real Rate.
- Habit Persistence Also Helpful for Understanding Asset Prices

- Flow Budget Constraint (Ignoring Insurance Considerations):

$$\begin{aligned}
 M_{t+1} &= R_t [M_t - Q_t + (\mu_t - 1)M_t^a] \\
 &\quad + Q_t + P_t w_t l_t + P_t r_t^k u_t \bar{k}_t + D_t \\
 &\quad - P_t (c_t + i_t + a(u_t) \bar{k}_t) \\
 k_t &= u_t \bar{k}_t, \text{ capital services} \\
 \bar{k}_{t+1} &= (1 - \delta) \bar{k}_t + F(i_t, i_{t-1})
 \end{aligned}$$

$Q_t$  ~cash balances

$M_t$  ~beginning-of-period  $t$  Household Money

$M_t^a$  ~beginning-of-period  $t$  Aggregate Money

$D_t$  ~profits

$\mu_t$  ~gross money growth rate

$M_t - Q_t + (\mu_t - 1)M_t^a$  ~deposits at financial intermediary

$a(\cdot)$  ~costs of utilizing capital more intensively

$u_t$  ~utilization rate of capital

$F(i_t, i_{t-1})$  ~cost of adjusting investment

$k_t$  ~capital services

$\bar{k}_t$  ~physical capital.





## Structure of the Labor Market

- Intermediate Good Firms Use Labor Aggregate:

$$L_t = \left[ \int_0^1 h_{j,t}^{\frac{1}{\lambda_w}} dj \right]^{\lambda_w} .$$

- Price of  $L_t$  :

$$W_t = \left[ \int_0^1 (W_t(i))^{\frac{1}{1-\lambda_w}} di \right]^{1-\lambda_w} .$$

- Demand for Household Labor Service,  $h_{j,t}$  :

$$h_{j,t} = \left( \frac{W_t}{W_{j,t}} \right)^{\frac{\lambda_w}{\lambda_w-1}} L_t, \quad 1 \leq \lambda_w < \infty .$$

$W_{j,t}$  ~ wage set by household

$L_t$  ~ homogeneous aggregate labor

$W_t$  ~ wage rate of aggregate labor



## Calvo-style Wage Setting:

- With Probability  $1 - \xi_w$ ,  $i^{th}$  Household Sets Wage,  $W_{it}$ , Optimally, to  $\tilde{W}_t$ .
- With Probability  $\xi_w$ ,

$$W_{it} = \pi_{t-1} W_{i,t-1}, \quad \pi_t = \frac{P_t}{P_{t-1}}.$$

- First Order Condition:

$$E_{t-1} \sum_{l=0}^{\infty} (\xi_w \beta)^l h_{j,t+l} \left[ \psi_{t+l} \frac{\tilde{W}_t X_{t,l}}{P_{t+l}} - \lambda_w z_{h,t+l} \right] = 0.$$

$\frac{\psi_t}{P_t}$  value of one dollar (Multiplier on Budget Constraint)

## Cash Balance Decision, $Q_t$

- Households Set  $Q_t$  To Maximize Utility

$$v' \left( \frac{Q_t}{P_t} \right) \frac{1}{P_t} + \frac{\psi_t}{P_t} = \frac{\psi_t}{P_t} R_t,$$

- $Q_t/P_t$  Decreasing in  $R_t$ .
- Liquidity Effect Due to This Equation.
  - $c_t, i_t, Y_t, L_t, P_t, W_t$  Predetermined Relative to Monetary Shock
  - Loan Market Clearing:

$$W_t L_t = \mu_t M_t - Q_t$$

- $Q_t$  Must Absorb all Money Injections.
  - Can Only Happen With Fall in  $R_t$ .
- This is a ‘Limited Participation Story’
  - But With A Different Twist

# Consumption Decision

$$E_{t-1} \frac{u_{c,t}}{P_t} = \beta E_{t-1} \frac{u_{c,t+1}}{P_{t+1}} R_{t+1}.$$

# Capital Utilization Decision

$$E_{t-1} u_{c,t} [r_t^k - a'(u_t)] = 0$$

- Why Have Variable Capital Utilization?
- Motivation I:
  - In Data,  $Y/L$  Rises after Expansionary Monetary Policy Shock.
  - Standard Model:  $L \uparrow \Rightarrow \frac{Y}{L} \downarrow$
  - One Resolution:  
Distinguish Physical Stock of Capital,  $\bar{k}$ , and Services from Capital,  $u\bar{k}$ . If  $u \uparrow$  when  $L \uparrow$ , maybe  $\frac{Y}{L} = \left(\frac{u\bar{k}}{L}\right)^\alpha \uparrow$
- Motivation II:  
Variable Capacity Utilization Reduces Upward Pressure On Rental Rate of Capital and, hence, on Marginal Costs After Expansionary Monetary Policy Shock.

# Investment and Adjustment Costs

- Why Do We Need Costs of Adjusting Capital?
- Rate of Return on Capital:

$$R_t^k = \frac{r_{t+1}^k + P_{k',t+1}(1 - \delta)}{P_{k',t}},$$

$P_{k',t} \sim$  consumption price of installed capital

$\delta \in (0, 1) \sim$  depreciation rate.

$r_{t+1}^k = s_{t+1}MP_{t+1}^k$ , rental rate on capital

$MP_t^k \sim$  marginal product of capital

$s_{t+1} = \frac{MC_t}{P_t} = \frac{1}{\text{markup}}$

- Almost Any Model,

$$\frac{R_t}{\pi_{t+1}} \approx R_t^k = \frac{r_{t+1}^k + P_{k',t+1}(1 - \delta)}{P_{k',t}}.$$

- So, If a Positive Money Shock Drives Down Real Rate, Then

$$R_t^k \downarrow$$

- This is Trouble For Standard Models ( $P_{k',t} = 1, s_t = 1$ ):

$$R_t^k \text{ down requires } MP_t^k \text{ down}$$

- Problem:

$MP^k$  down Requires Surge in Investment, especially with employment up.



- With Adjustment Costs, No Surge in Investment
- Cost-of-Change Adjustment Costs:

$$k' = (1 - \delta)k + F\left(\frac{I}{I_{-1}}\right)I$$

Good for ‘Hump-shaped Investment Response’.

- Other Reasons for Interest in Adjustment Costs:
  - Important for Understanding Asset Prices.
  - Necessary for Movements in Price of Capital.

# Investment Decision

- Household Owns the Capital Stock and Carries Out Capital Accumulation.
- Technology for Capital Accumulation:

$$\bar{k}_{t+1} = (1 - \delta)\bar{k}_t + F(i_t, i_{t-1}),$$

$$F(i_t, i_{t-1}) = (1 - S \left( \frac{i_t}{i_{t-1}} \right))i_t.$$

- Euler Equation for  $\bar{k}_{t+1}$ :

$$E_{t-1}\psi_t = \beta E_{t-1}\psi_{t+1} \frac{u_{t+1}r_{t+1}^k - a(u_{t+1}) + P_{k',t+1}(1 - \delta)}{P_{k',t}}.$$

$P_{k',t}$  ~marginal cost, in units of consumption goods,  
of installed, physical capital

- Euler Equation for  $i_t$ :

$$E_{t-1}\psi_t = E_{t-1} [\psi_t P_{k',t} F_{1,t} + \beta \psi_{t+1} P_{k',t+1} F_{2,t+1}].$$

- After linearization:

$$\hat{i}_t = \hat{i}_{t-1} + \frac{1}{S''} \sum_{j=0}^{\infty} \beta^j E_{t-1} \hat{P}_{k',t+j}.$$

## Empirical Factors Underlying Model Design and Estimation Results

- Contemporaneous Impact of Positive Money Shock:  $P$  and  $Y$  Don't Change,  $R$  Falls.
- Positive Monetary Shock Has Hump-Shape Impact on Investment, Consumption, Output and Employment.
- Positive Monetary Shock Has Hump-Shape Impact on Productivity.
- Positive Monetary Shock Drives Up Output, and Has Little Impact on Prices.

## Contemporaneous Impact of Positive Money Shock

- Quantity and Price Decisions Predetermined Relative to Monetary Policy Shock.
- Household Portfolio Decisions Taken After Monetary Shock.
  - Limited Participation
  - To Absorb the Extra Liquidity,  $R$  Must Fall

## Positive Monetary Shock Has Hump-Shape Impact on Investment, Consumption, Output and Employment

- Low Real Interest Rate After Positive Monetary Shock Raises Incentive to Invest
  - Investment Adjustment Costs Put Hump-Shape Pattern in Investment Response
- Habit Persistence in Preferences Put Hump in Consumption.
  - $U(c - bc_{-1})$
- Hump In Investment and Consumption Produces Hump in Output.

## Positive Monetary Shock Has Hump-Shape Impact on Productivity

- Production Function:

$$Y = K^\alpha L^{1-\alpha} - \phi$$

- Labor Productivity:

$$\begin{aligned} \frac{Y}{L} &= \left(\frac{K}{L}\right)^\alpha - \frac{\phi}{L} \\ &= \left(\frac{uk}{L}\right)^\alpha - \frac{\phi}{L} \end{aligned}$$

- Positive Money Shock Drives  $Y/L$  Up Because of:
  - Variable Capital Utilization
  - Fixed Cost in Production,  $\phi$

## Recap: Positive Monetary Shock Drives Up Output, and Has Little Impact on Prices

- Price-Markup Behavior of Firms:

$P =$  marginal cost(labor cost, capital rental cost)

- sticky wages prevent a rise in labor costs after positive money shock
- variable capital utilization prevents a rise in capital costs after positive money shock

- Households

$$U(c, \frac{M}{P})$$

- $M$  up Implies  $M/P$  up.
- With Rise in  $M/P$ , Demand More  $c$ .



- Rise in  $c$  Demanded Drives up Output.

## Reduced Form Expression for Inflation in Model

$$\hat{\pi}_t = \frac{1}{1 + \beta} \hat{\pi}_{t-1} + \frac{\beta}{1 + \beta} E_{t-1} \hat{\pi}_{t+1} + \frac{(1 - \beta \xi_p)(1 - \xi_p)}{(1 + \beta) \xi_p} E_{t-1} \hat{s}_t,$$

- Or:

$$\hat{\pi}_t = \hat{\pi}_{t-1} + \frac{(1 - \beta \xi_p)(1 - \xi_p)}{\xi_p} E_{t-1} \sum_{j=0}^{\infty} \beta^j \hat{s}_{t+j}$$

- Damped Inflation Response Requires Damped Marginal Cost Response.
- Econometric Estimates Emphasize Model Features That Mute Response of Marginal Cost to Shocks.

## Next:

- Assigning Parameter Values
- Analysis of Quantitative Model

# Econometric Methodology

Three Types of Parameters:

- Parameter Set 1: Parameters that Do Not Enter Formal Estimation Criterion.
- Parameter Set 2: Parameters that Govern Monetary Policy.
- Parameter Set 3: Parameters Estimated Using Estimated Impulse Response Functions.

Parameter Set 1: Parameters that Don't		
Enter Formal Estimation Criterion		
discount factor	$\beta$	$1.03^{-.25}$
capital's share	$\alpha$	0.36
capital depreciation rate	$\delta$	0.025
markup, labor suppliers	$\lambda_w$	1.05
mean, money growth	$\mu$	1.017
labor utility parameter	$\psi_0$	set to imply $L = 1$
real balance utility parameter	$\psi_q$	set to imply $Q/M = 0.44$
fixed cost of production	$\phi$	set to imply ss profits = 0

## Parameter Set 2: Parameters Characterizing Monetary Policy

$$\mu_t = \mu + \theta_0\varepsilon_t + \theta_1\varepsilon_{t-1} + \theta_2\varepsilon_{t-2} + \dots$$

where

$$\mu_t = \log \frac{M_t}{M_{t-1}}.$$

Parameters Taken From Estimated Response of  $\mu_t$  to  $\varepsilon_t$ .

- Parameter Set 3:

$$\gamma \equiv (\lambda_f, \xi_w, \xi_p, \sigma_q, S'', b, \sigma_a).$$

- Estimation Criterion:

$$J = \min_{\gamma} (\hat{\psi} - \psi(\gamma))' V^{-1} (\hat{\psi} - \psi(\gamma)),$$

- $\psi(\gamma)$  model impulse responses
- $\hat{\psi}$  estimated impulse responses from VAR
- $V$  estimate of sampling uncertainty in  $\hat{\psi}$   
(actually, we used the diagonal part of  $V$  only)

ESTIMATED PARAMETER VALUES							
Model	$\lambda_f$	$\xi_w$	$\xi_p$	$\sigma_q$	$S''$	$b$	$\sigma_a$
Benchmark	1.46 (.16)	.70 (.07)	.50 (.23)	9.66 (.78)	3.60 (2.24)	.63 (.14)	.01

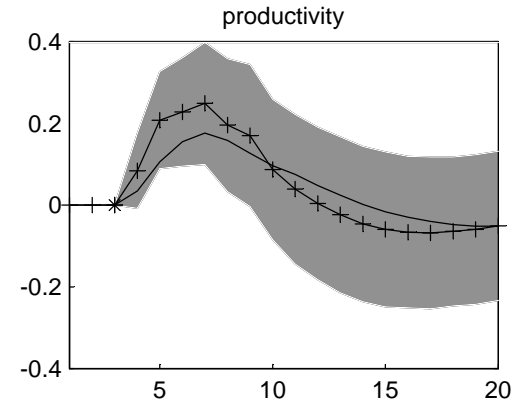
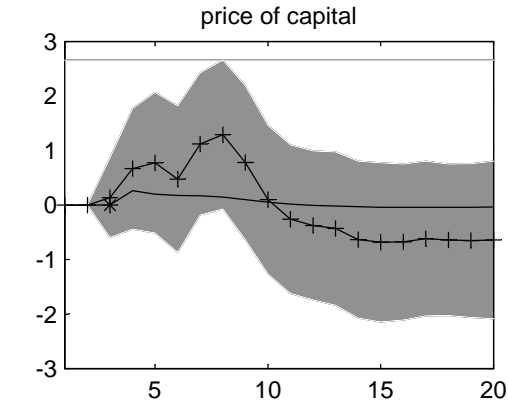
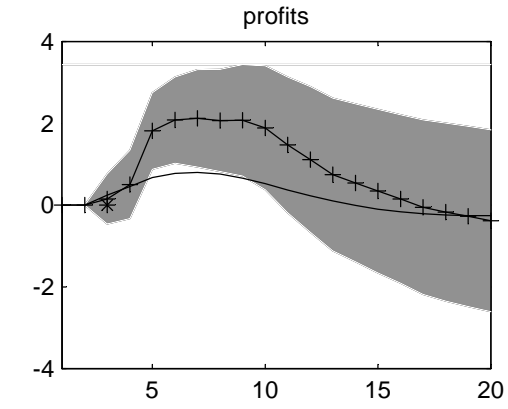
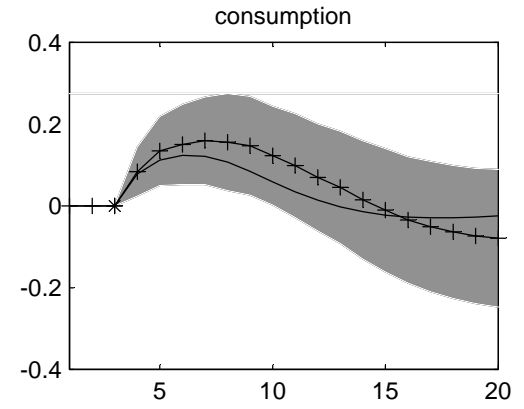
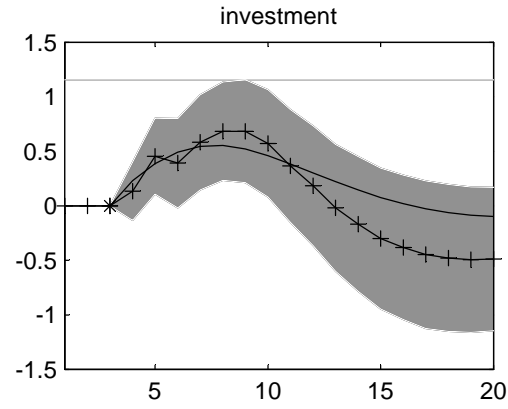
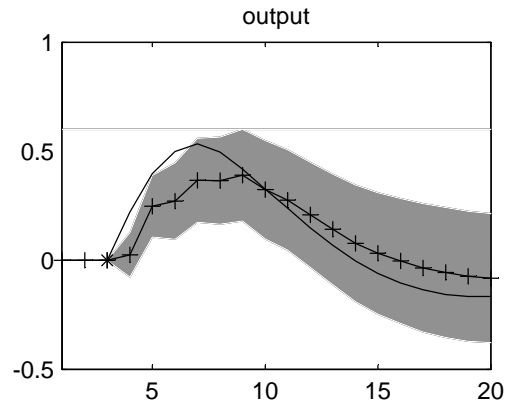
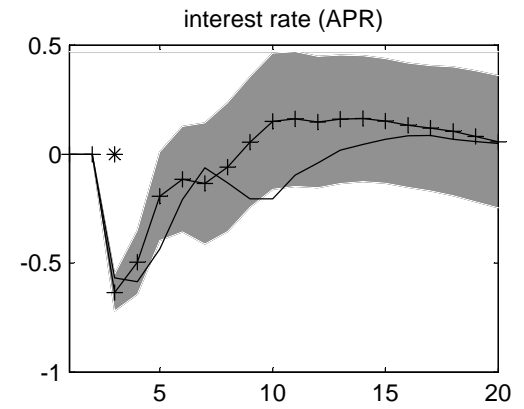
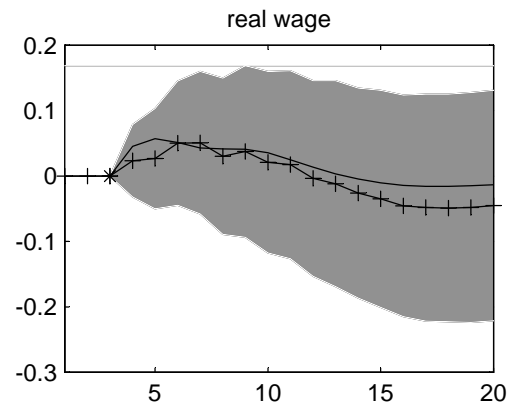
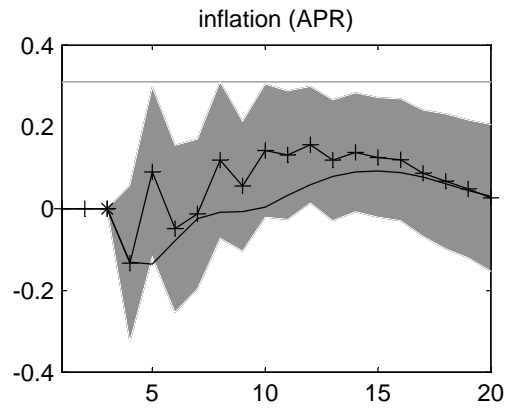
- Properties of Estimates:
  - $\xi_w \rightarrow$  wage contracts last 3.3 quarters
  - $\xi_p \rightarrow$  price contracts last 2 quarters
  - $\xi_p$  ‘less important’ than  $\xi_w$
  - $\sigma_q$  implies  $-d \log q / dR = 1.05$
  - $\sigma_a$  small  $\rightarrow$  capital rental rate constant
  - Habit a Little Lower Than B-C-F
  - $\lambda_f$  Consistent with Rotemberg-Woodford (1995)



## Properties of Estimated Model

- Model Does Well Statistically
- Enormous Inflation Inertia: Takes 3 Years to Start Rising
- Persistence in Output: Peak Effect In One Year.
- Hump-shaped response of Output, Investment, Consumption, Labor Productivity.
- Large, Persistent Liquidity Effects.
- Small Real Wage Response.
- Model Has Much Internal Propagation.

Figure 1: Model and Data Impulse Responses



# Conclusion

A Model Was Displayed, Which Accounts for the Salient Features of What Happens After a Monetary Policy Shock.

- Sticky Wages and Variable Capital Utilization Generates ‘Inflation Inertia’ and ‘Output Persistence’.
- Habit Persistence and Investment Adjustment Costs Generate Hump-Shaped Investment, Output, Consumption Responses.
- Fixed Costs and Variable Capital Utilization Generate Hump-Shaped Labor Productivity Response.